



1 **A low-cost acoustic permeameter**

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8 **Abstract.** Intrinsic permeability is an important parameter that regulates air exchange through porous media such as snow.
9 Standard methods of measuring snow permeability are inconvenient to perform outdoors, fraught with sampling errors and
10 require specialized equipment, while bringing intact samples back to the laboratory is also challenging. To address these
11 issues, we designed, built, and tested a low-cost acoustic permeameter that allows computation of volume-averaged intrinsic
12 permeability for a homogenous medium. Permeameter elements were designed for use in snow but the measurement
13 methods are not snow-specific. The electronic components, consisting of a signal generator, amplifier, speaker, microphone
14 and oscilloscope, are inexpensive and easily obtainable. The system is suitable for outdoor use when it is not precipitating
15 but the electrical components require protection from the elements in inclement weather. The permeameter can be operated
16 with a microphone either internally mounted or buried a known depth in the medium. The calibration method depends on
17 choice of microphone positioning. For an externally located microphone, calibration was based on a low-frequency
18 approximation applied at 500 Hz that provided an estimate of both intrinsic permeability and tortuosity. The low-frequency
19 approximation that we used is valid up to 2 kHz but we chose 500 Hz because data reproducibility was maximized at this
20 frequency. For an internally mounted microphone, calibration was based on attenuation at 50 Hz and returned only intrinsic
21 permeability. We found that 50 Hz corresponded to a wavelength that minimized resonance frequencies in the acoustic tube
22 and was also within the response limitations of the microphone. We used reticulated foam of known permeability (ranging
23 from $2 \times 10^{-7} \text{ m}^2$ to $3 \times 10^{-9} \text{ m}^2$) and estimated tortuosity of 1.05 to validate both methods. For the externally mounted
24 microphone the mean normalized standard deviation was 6% for permeability and 2% for tortuosity. The mean relative error
25 from known measurements was 17% for permeability and 2% for tortuosity. For the internally mounted microphone the
26 mean normalized standard deviation for permeability was 10% and the relative error was also 10%. Permeability
27 determination for an externally mounted microphone is less sensitive to environmental noise than is the internally mounted
28 microphone and is therefore the recommended method. The approximation using the internally mounted microphone was
29 developed as an alternative for circumstances in which placing the microphone in the medium was not feasible.
30 Environmental noise degrades precision of both methods and is recognizable as increased scatter for replicate data points.



1 Introduction

2 Intrinsic permeability is the proportionality constant in Darcy's Law that describes the interconnectedness of air
3 space in permeable media such as snow. It has long been recognized as an important parameter that regulates air exchange
4 both within the snow pore space and between the atmosphere and the snowpack (Bader, 1939). Since permeability is difficult
5 to measure directly, early efforts focused on developing empirical relationships that describe permeability as a function of
6 more easily measured parameters such as snow density (Bender, 1957; Shimizu, 1970; Martinelli, 1971). These convenient
7 formulations may be accurate for the specific snow conditions used to establish the empirical formula but often fail for other
8 snow conditions (Domine et al., 2013). In an effort to obtain more accurate field measurements of permeability several
9 experimental efforts employed vacuum flow-through devices (Conway & Abrahamson, 1984; Chacho & Johnson, 1987;
10 Hardy & Albert, 1993; Albert et al., 2000; and Courville et al., 2007). However, flow-through measurements are time
11 consuming and fraught with potential sampling errors and alteration of the sample from its native condition (Sommerfeld &
12 Rocchio, 1993). Some sampling issues have been resolved by sample extraction and examination in a lab environment to
13 measure pore space in terms of specific surface area by X-ray tomography and gas adsorption techniques (Kerbrat et al.,
14 2008). But this multi-step process requires specialized equipment and still does not resolve issues of small-scale spatial
15 heterogeneity and sample size representativeness (Albert, 2001).

16 In this paper, we describe the design, construction, and calibration of an *in-situ* active acoustic device that samples a
17 measurement volume larger than that obtainable with current flow-through devices to acquire a volume-averaged estimate of
18 intrinsic permeability. Active sampling methods of snow properties have been successfully applied in previous studies. For
19 example, Albert et al. (2007) measured the evolution of an acoustic pulse, generated by firing a pistol blank, and compared
20 the pulse shape with that of a simulated pulse to estimate volume-averaged permeability of an Alaskan snowpack. Kinar and
21 Pomeroy designed (2007) and improved (2015) upon an active acoustic device that infers properties such as snow water
22 equivalent from the differential backscatter at frequencies between 20 Hz and 10 kHz. The two methods that we present are
23 less sophisticated than either the Albert or Kinar methods but have the advantage that no specialized equipment is required.
24 Our design borrows elements from Ishida (1965), Buser (1986), and Moore et al. (1991).

25 Method

26 2.1 Design and Assembly of the Acoustic Permeameter

27 We assembled an acoustic permeameter from commonly available parts (Fig. 1). A Heathkit Model IG-1275 signal generator
28 produced a sine wave of a specified frequency and amplitude that was split and directed both to channel 1 of a Tektronix
29 TDS 1001 oscilloscope and to a 4Ω Altec A4468 speaker. Electrical components were powered from a DC-AC inverter and
30 12V car battery. The speaker was screw-mounted onto a ring of 3/4-in-thick medium-grade plywood. An acoustic tube was
31 constructed using 20-cm (inside) diameter, schedule 40 PVC pipe. The acoustic tube was vertically mounted onto the



1 plywood ring and secured with butterfly clamps. During measurement, the tube was placed on the medium of interest with
2 the speaker facing downward such that sine waves emanating from the speaker would interrogate the medium. The
3 subsequent acoustic response was captured by a Radio Shack™ unidirectional microphone (model 3303038, frequency
4 range: 50 Hz-15 kHz) and directed to the second input channel on the oscilloscope. Frequency and amplitude of input and
5 output signals were stored on the oscilloscope USB drive. We do not have full knowledge of the characteristics of the
6 microphone transducer. However, the calibration is empirical and will vary with each microphone so discrepancies between
7 microphones are accommodated by the calibration.

8 2.2 Acoustic Permeability Determination – External Microphone Method

9 The first method used to measure intrinsic permeability involved using an externally placed microphone (EM), where we
10 placed the test media between the sound source and the microphone. The calibration setup for the EM method is similar to
11 Fig. 1 but with the speaker mounted in an upward orientation and the microphone mounted directly above the centerline of
12 the PVC tube, facing downward. Acoustic intensity at a given frequency was measured with the microphone in open air to
13 establish reference amplitude. Then a foam sample was placed over the end of the speaker tube and weighted at the edges to
14 minimize sample vibration. At each applied frequency, attenuation and phase shift were determined by comparison with the
15 reference measurement. We then utilized the low-frequency approximation in Moore et al. (1991, hereafter referred to as
16 M91), to calculate permeability. In M91, estimates of tortuosity (τ) and effective flow resistivity (σ_{pe}) were iteratively
17 adjusted until optimal agreement between the measured and modeled value for the propagation constant (k_b) at a given
18 frequency (f) was obtained. Snow permeability (k) can then be computed from flow resistivity given knowledge or
19 assumptions of the snow grain shape. The theoretical basis for the M91 low-frequency approximation is described in Sect.
20 3.1 of this paper. An added benefit of this method relative to a flow-through permeameter is that it produces a measure of
21 tortuosity as well as permeability.

22 2.3 Acoustic Permeability Determination – Internal Microphone Method

23 A second permeability measurement method employed the microphone mounted inside the acoustic tube, facing outward, at
24 a fixed position (15 cm) from the open end. We refer to this as the IM method. We measured attenuation at 50 Hz relative to
25 an open-air value with the open end of the acoustic tube snug against the test media. At this frequency, the wavelength of the
26 emitted frequency is much greater than the length of the acoustic tube. Since the medium represents an acoustic barrier to the
27 emitted waveform, the amplitude of the transmitted waveform was progressively retarded as permeability increased.
28 Simultaneously, the amplitude of the reflected waveform, measured by the internally mounted microphone, increased. From
29 Morse (1952, hereafter referred to as M52) attenuation at a given frequency is a function of flow resistivity. Amplitude of the
30 reflected waveform is inversely proportional to the amplitude of the transmitted waveform so permeability was computed as
31 a function of the ratio between the initial amplitude and the reflected amplitude.



1 2.4 Flow-through Permeability Determination

2 We verified acoustic permeameter measurements with 5-cm-thick reticulated foam samples. The permeability of these foam
 3 samples was established with a flow-through permeameter similar to Albert et al. (2000) with the exception that we utilized
 4 three high-precision (Paroscientific 216B) absolute pressure sensors rather than two relative pressure sensors (Fig. 2). Using
 5 absolute pressure sensors rather than relative pressure sensors required a modification of Albert's method so we briefly
 6 describe our alternate method. For each foam type we cut a cylindrical section and spread a layer of petroleum gel around the
 7 cut edge. We then slid the cut foam into the double-walled permeameter until the inner face of the foam was flush against the
 8 inner wall of the permeameter as shown in Fig. 2. The gel sealed gaps between the foam and vessel wall. We cross-calibrated
 9 the three pressure sensors before initiating airflow through the permeameter. The three pressure sensors monitored
 10 atmospheric, inner cylinder, and outer cylinder pressures. Following Albert et al. (2000), we acquired the pressure drop
 11 across each foam sample at 8-12 flow rates while adjusting a valve to regulate the pressure between the inner and outer
 12 vessel to eliminate radial flow. We used the slope of the subsequent flow rate vs. pressure drop curve to derive permeability
 13 from Darcy's law valid for Reynolds numbers less than 1:

$$14 \quad k = \frac{Q L \mu}{\Delta P A}, \quad (1)$$

15 where k is intrinsic permeability (m^2), Q is volumetric discharge ($\text{m}^3\text{-s}^{-1}$), A is the sample surface area (m^2), L is the sample
 16 height (m), ΔP is the pressure drop (Pa) and μ is dynamic air viscosity ($\text{kg}\cdot\text{m}^{-1}\cdot\text{s}^{-1}$). Our samples were distinct in properties
 17 from those published by Clifton et al. (2008) (Table 3.1), suggesting that intrinsic permeability of reticulated foam with the
 18 same specified pores per linear inch (PPI) but different manufacturers (here Regicell and FXI Corporation) must be
 19 determined experimentally. Permeability measured for the FXI samples in Table 3.1 span expected snow permeability values
 20 ranging from lightly compacted snow (low permeability) to depth hoar (high permeability), (Arakawa et al., 2009).

21 3 Theory

22 In this section, we describe the theoretical basis for the two methods used to acoustically measure snow permeability.

23 3.1 Theory for the EM Method

24 The complex propagation constant for sound through permeable media can be written in general terms as:

$$25 \quad k_b = a + ib \quad (2)$$

26 Coefficients of the propagation constant define the phase and magnitude of attenuation, respectively, and are defined in M91
 27 as:

$$28 \quad a = \frac{\pi \Delta \phi}{180 d} \quad (3)$$

$$29 \quad b = \frac{\text{Attenuation}(dB) \ln(10)}{20d} \quad (4)$$



1 where $\Delta\phi$ is the phase shift between a free air measurement and the in-snow measurement and d is media thickness. We
 2 measure attenuation in terms of a voltage difference between the input (V_{IN}) and output signal (V_{OUT}) as:

$$3 \text{ Attenuation}(dB) = 20 \log_{10} \left(\frac{V_{OUT}}{V_{IN}} \right) \quad (5)$$

4 Attenborough (1983) developed a four-parameter acoustic model that describes acoustic attenuation through permeable
 5 media. These four parameters: porosity, effective flow resistivity, pore shape factor and grain shape factor collapse to two
 6 parameters in the low-frequency approximation given in M91:

$$7 k_b = 0.0079\sqrt{f} [9.10 \tau f + i4\sigma_{pe}]^{0.5} \quad (6)$$

8 The M91 authors used Eq. (6) to calculate the propagation constant for a given tortuosity and flow resistivity and Eqs. (2-5)
 9 to calculate the propagation constant from phase shift and attenuation. Values for flow resistivity and tortuosity in Eq. (6)
 10 were iteratively adjusted until the difference between the propagation constant determined by these two methods was
 11 minimized. Due to environment-dependent nonlinear responses at both low and high frequencies the M91 authors obtained
 12 the best fit when they used well chosen point measurements rather than measurements over a range of frequencies. Similarly,
 13 our results are based on well-chosen point measurements. But instead of iteratively solving Eq. (6) we separate the real and
 14 imaginary parts to independently solve for tortuosity and effective flow resistivity:

$$15 \tau = \frac{[a^2 - b^2]}{[9.10][0.0079]^2 f^2} \quad (7)$$

$$16 \sigma_{pe} = \frac{ab}{2[0.0079]^2 f} \quad (8)$$

17 We then apply empirical calibrations to match derived tortuosity and effective resistivity with known values.

18 3.2 Theory for the IM Method

19 With the alternate configuration of the microphone placed inside the acoustic tube, Eqs. (2-8) are no longer applicable.
 20 Instead, we use an alternate theoretical basis to determine intrinsic permeability based on results described in M52. M52
 21 found and Ishida (1965) verified a simple relationship between flow resistivity and signal attenuation:

$$22 \alpha = \beta\sqrt{\omega\sigma} \rightarrow \sigma = \frac{\alpha^2}{2\pi f} \times 10^n \quad (9)$$

23 where α is an attenuation constant, β is an empirical constant, ω is the imposed angular frequency and σ is flow resistivity.
 24 As with the EM method, we fit a sine wave to the input and output signals to eliminate white noise and then determined the
 25 phase offset and attenuation between the input and output signals as a function of the input frequency. Instead of measuring
 26 the attenuation through the media, we measure the amplitude of the reflected waveform at 50 Hz. We take the amplitude of
 27 the reflected acoustic energy as an empirically-derived function of transmitted acoustic energy. Using reticulated foam
 28 samples of known permeability, we relate the ratio of the reflected signal amplitude to initial signal amplitude with flow-
 29 through permeability measurements.



1 4 Results

2 4.1 Results for the EM Method

3 Having calibrated permeability of the reticulated foam samples with the flow-through permeameter (in Fig. 2) we
4 subsequently obtained acoustic measurements by the EM method. Three replicates were acquired for each foam sample at
5 each frequency. After some experimentation, we opted to utilize data acquired at 500 Hz because this frequency lies within
6 the valid range of frequencies for the low-frequency approximation and because the 500 Hz results were more replicable
7 than those acquired at higher frequencies.

8 In M91 flow resistivity and tortuosity were determined by iteratively finding the best fit between measurements given in
9 Eqs. (2-5) and the theoretical prediction given in Eq. (6). Since we know *a priori* the foam tortuosity and permeability we
10 compared the known effective flow resistivity with the effective flow resistivity computed from Eqs. (2-8). As in Albert
11 (2007) and using a pore shape factor ratio (s_f) of 1, the effective flow resistivity as derived from permeability is:

$$12 \sigma_{pe} s_f^2 = \frac{\mu}{k} \quad (10)$$

13 For the foam samples, we found that a linear fit resolved the difference between computed and known flow resistivity for a
14 given permeability. In short, acoustically derived effective flow resistivity did not match the actual effective flow resistivity
15 but deviated by a linear function from it. Therefore, from Eq. (10), we computed flow resistivity is a linear function of
16 permeability.

17 In Fig. 3 we plotted the results of three independent data sets, each data set corresponding to a different volume setting on
18 the signal generator and rendered in a different color. For a given data set, the signal generator volume was established for
19 the first data point and not changed for the remaining data points. Data corresponding to the blue/black/red data sets had
20 initial imposed volume that associated to RMS signal input voltages of 1.3/2.3/5.6V, respectively. Plotted in log/log format,
21 data points for each data set in Fig. 3 are roughly collinear and the slope of the best-fit line for a given data set is nearly
22 parallel to the other two data sets but the data sets are not coincident (Fig. 4). This result indicates that as the amplitude of
23 the imposed sine wave was increased, absolute attenuation of the signal also increased. Since the acoustically derived
24 permeability is sensitive to the amplitude of the imposed waveform, it is therefore important to use the same amplitude
25 waveform in the calibration as in subsequent permeability measurements. The relationship between σ_{pe} and k reversed at the
26 highest permeability in Fig. 3. The reason for this reversal is possibly attributable to non-linearity in microphone response
27 and represents an upper limit to the permeability that can be measured by this technique within the constraints of our
28 experimental design. Triplicate data points were nearly coincident in most cases; however, the blue and black asterisks in
29 Fig. 3 correspond to points that were more than a standard deviation removed from the other two points in the given
30 triplicate measurement. Differences in the imposed amplitude for these two data points does not account for their deviation
31 from the mean suggesting the source of error was environmental. These data were acquired outdoors in a relatively quiet but
32 acoustically uncontrolled location so we attribute this error is to intermittent external noise. It is therefore also important to
33 acquire multiple data points for each measurement so that one can distinguish the impact of incidental, external noise.



1 Uncalibrated tortuosity calculated for different foam samples was nearly very similar but unrealistically high with an average
2 of 17.7 and standard deviation of 1.54 between all of the samples. A slight but monotonic decrease in measured tortuosity
3 with decreasing permeability accounted for most of the standard deviation as opposed to random scatter. For comparison,
4 analogous data from Alvarez-Arenas et al. (2006), Kino et al. (2012) and references in Melon and Castagnede (1995) and
5 Doutres and Atalla (2012) note that reticulated foam commonly has a narrow range of tortuosity from 1.03 to 1.06.
6 Tortuosity of the FXI reticulated foam is not independently measured but shares other specifications with these other sources
7 and likely has tortuosity in the same range.

8 We empirically compensate for the differences between the theoretical and experimentally derived values for tortuosity and
9 effective flow resistivity. Our rationale is that the functional relationships between the theoretically and derived values for
10 tortuosity and effective flow resistivity are the same so the differences in values can be resolved by a first-order calibration.
11 Calculated tortuosity depended very weakly on media permeability so multiplying the calculated tortuosity by an
12 empirically-derived constant renders the theoretical value. On the other hand, calculated permeability varies linearly (on a
13 log scale) with effective flow resistivity (as shown in Fig. 4) so a linear calibration is required to calculate permeability from
14 measured effective flow resistivity. The multiplicative constant for tortuosity is found by dividing the mean known tortuosity
15 by the mean derived tortuosity. The linear calibration relating effective flow resistivity to permeability is taken from the
16 slope of the line in Fig. 4. In practice, one must calibrate the acoustic permeameter with media of known permeability and
17 tortuosity to derive these multiplicative constants. Once these multiplicative constants have been determined for the acoustic
18 permeameter, the tortuosity and permeability of other media having similar impedance can be derived without *a priori*
19 knowledge of media tortuosity or permeability. For the 5.6V data set we find the multiplicative constant as: $\alpha = 0.057$. For
20 the same data set a linear fit between measured flow resistivity and known permeability is given by:

$$21 \log_{10}(k) = -2.0219 \times \log_{10}(\sigma_{pe}) - 0.1764 \quad (11)$$

22 With these modifications, the M91 method obtains derived tortuosity ranging from 1.02 to 1.07 for the foam samples with a
23 standard deviation of ± 0.03 . Percentage normalized standard deviation for permeability measurements ranged from 2.1% for
24 the Z80 foam to 11.6% for the Z30 foam with a mean of 6.2% across all foam samples. We normalize the standard deviation
25 because this error measure does not change when effective flow resistivity is calibrated with a multiplicative constant. The
26 average percentage error between known and derived permeability was 17% by the EM method.

27 4.2 Results for the IM method

28 Applying Eq. (9) to results obtained with the microphone placed inside the acoustic tube at 50 Hz, 100 Hz, and 250 Hz
29 yielded results shown in Fig. 5. Since we are measuring reflected acoustic energy rather than transmitted energy the result
30 shown in Fig. 5 is an indirect (relative) measure of flow resistivity. Triplicates were acquired for each foam sample and these
31 data were highly reproducible as shown by the close grouping of each triplicate. Data at these three frequencies were
32 acquired on different days, each with a slightly different amplitude baseline (free air) setting, accounting for the horizontal
33 displacement between curve fits. The percentage normalized standard deviation for 50 Hz measurements ranged from 0.45%



1 for the Z50 sample to 19% for the highest permeability (Z10) sample with a mean of 10% across all foam samples. The
2 average percentage error between known and derived permeability was 10% by the IM method. Since data at 50 Hz show
3 improved precision relative to 100 Hz and 250 Hz data, as given by the wider domain of reflected signal amplitude, we use
4 data at 50 Hz to compute permeability. The piecewise spline fit (black, in Fig. 5) describes the straight-line fit between
5 acoustically derived resistivity and the red dashed line delineates a smooth curve used to calibrate measurements to flow-
6 through permeability. There is a measurable phase shift with decreasing permeability of the test media, however, M52 does
7 not offer a relationship for tortuosity so none was attempted with this method. Microphone response limitations precluded
8 measurements below 50 Hz.

9 **4 Discussion**

10 Derived permeability using the EM and IM methods are compared with the flow-through (known) permeability in Fig. 6.
11 Intrinsic permeability for each foam sample is given in Table 3.1. Ideally, all measurements would fall on the diagonal line
12 in Fig. 6 meaning that acoustically measured permeability equals known permeability for each foam sample. We find
13 satisfactory agreement with known permeability for both acoustic methods. The average percentage error for the EM method
14 was 17% and 10% for the IM method. However, the curve fit for the IM method is nonlinear so a small error in effective
15 flow resistivity for a high permeability medium has a greater impact than the same error for a low permeability medium.
16 The EM and IM methods for determining permeability each have advantages and disadvantages. One advantage of the EM
17 method is that the function relating effective flow resistivity to permeability is linear, unlike the more complicated
18 relationship for the IM method. An advantage of a linear function is that a small error in measuring the x-coordinate yields
19 an error that is invariant with relative magnitude when determining the y-coordinate, regardless of the magnitude of the
20 measurement. This behavior is not true for non-linear functions such as the more complicated function employed in the IM
21 method. A disadvantage of the EM method is that it is not valid for high permeability media over the range of parameters
22 that we tested (e.g. 5 cm media thickness). The IM method suffers decreasing precision at high permeability because the
23 slope of the curve is increasing but, unlike the EM method, the curve fit remains valid. Data acquired using the IM method
24 was highly reproducible for all of our samples, which to some extent compensates for the slope-induced decrease in
25 precision at high permeability. Another potential disadvantage of the EM method is that the microphone must be placed in
26 the media to be measured. Depending on the circumstance, emplacement in the media may be difficult or impractical.
27 Finally, a disadvantage of the IM method is that it is more empirical than the EM method, which may limit its applicability
28 to different media types. Due to the linear functional form of the EM method, we suggest that it is the preferred method as
29 long as the media to be measured has a permeability that is within the valid range of measurements given by the calibration.
30 The results presented in this paper apply directly to reticulated foam, which has similar microphysical characteristics as snow
31 (Schneebeli and Sokratov, 2004; Clifton et al., 2008). Nevertheless, foam is not snow and we have yet to establish how
32 differences in characteristic impedance between reticulated foam and snow will affect signal attenuation measurements. The
33 next step is to validate acoustically derived measurements in snow by comparison with other methods. Given that



1 characteristic impedance of snow varies linearly with snow density (Marco et al., 1998) we anticipate that the calibration
2 curves for both the EM and IM methods will have similar shape to the curves in Figs. 4 and 5 but with a modified slope for
3 snow.

4

5 **5 Conclusions**

6 We conclude that it is feasible to derive intrinsic permeability with a low-cost acoustic permeameter by either the EM
7 method or the IM method. This system returns an unambiguous, volume-averaged permeability consistent with snow
8 densities ranging from lightly compacted snow to depth hoar. The EM method returned intrinsic permeability within 17% of
9 flow-through measurements and within 2% of comparable tortuosity measurements. The IM method returned intrinsic
10 permeability within 10% of flow-through measurements. Measurement reproducibility by the IM method is very high such
11 that the standard deviation between measurements is dwarfed by environmental factors such as background noise or
12 inhomogeneities in the media of interest. These methods are relevant in studies for which an expedient volume average
13 trumps a more detailed but time-consuming vertical profile that requires measuring multiple samples using a flow-through
14 permeameter. One significant advantage of using these methods is that a particular frequency is measured rather than a broad
15 spectrum. This feature obviates the need for specialized equipment used by other methods, such as a random noise generator
16 and a spectral recorder/analyzer. Disadvantages of this system are that measurements are affected by environmental
17 conditions such as background noise and wind. A future task is to validate this system by comparison with other measures of
18 intrinsic permeability over a range of snow habits and densities.

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- 12 Shimizu, H.: Air permeability of deposited snow, *Contrib. Inst. Low Temp. Sci. Ser. A* 22, 1-32, 1970.
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- 14 29, 2485–2490, 1993.
- 15



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2 **Table 1. Regicell foam permeability from Clifton et al. (2008) and FXI foam permeability measured with a flow-through**
3 **permeameter described in this paper.**

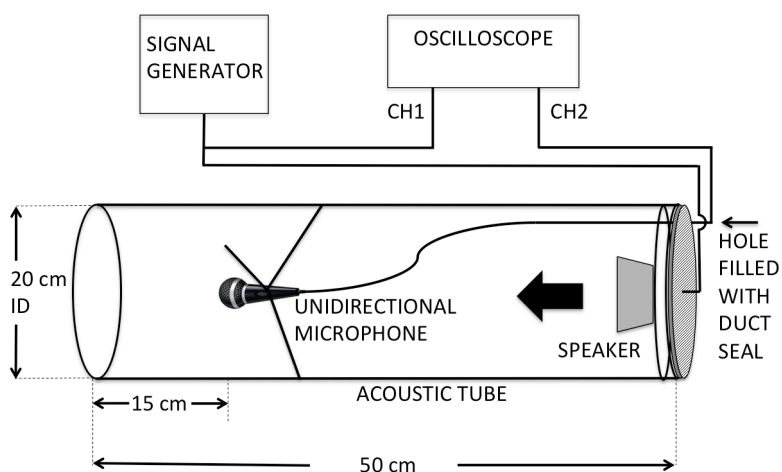
Foam Type	Flow-through Permeability (m ²)
Regicell 10	160 x 10 ⁻⁹
Regicell 30	39 x 10 ⁻⁹
Regicell 60	6 x 10 ⁻⁹
FXI Z10	206 x 10 ⁻⁹
FXI Z20	137 x 10 ⁻⁹
FXI Z30	47 x 10 ⁻⁹
FXI Z50	15 x 10 ⁻⁹
FXI Z80	3 x 10 ⁻⁹

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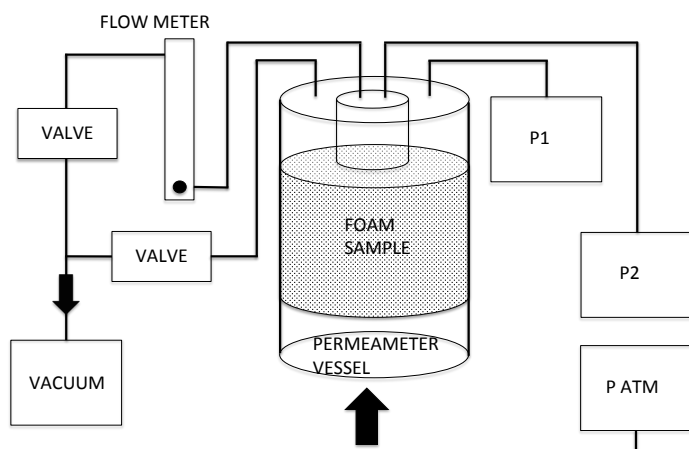


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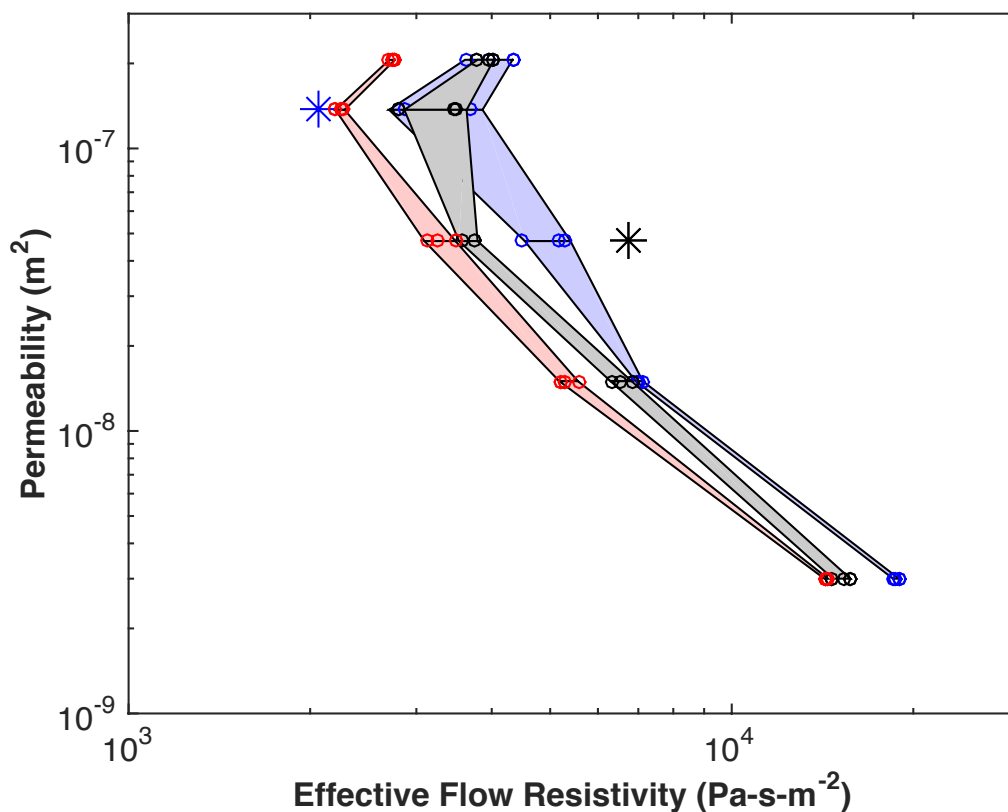
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Figure 1: Acoustic permeameter schematic.



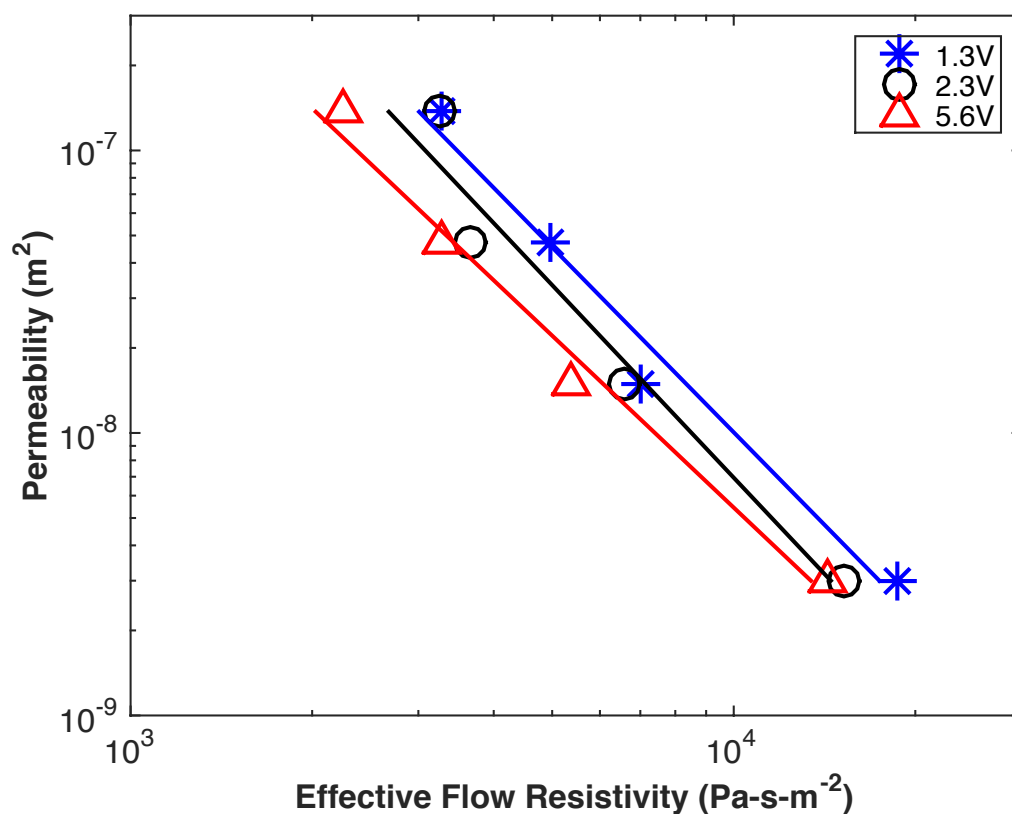
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Figure 2: Flow-through permeameter with three absolute pressure sensors labelled P1, P2, and P ATM.



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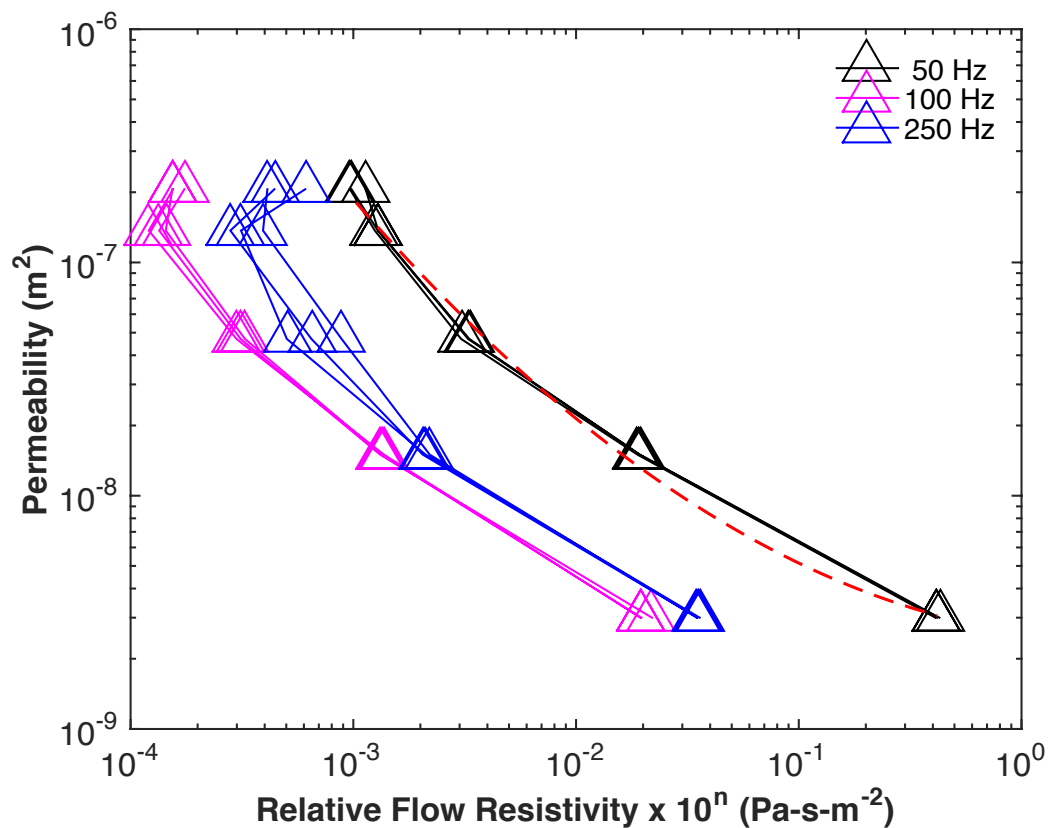
Figure 3: Comparison of acoustically derived permeability using M91 method at 500 Hz at three different initial conditions. The three initial conditions correspond to input RMS signal voltages of 1.3/2.3/5.6 volts highlighted in blue, black and red, respectively. Data was acquired outdoors on clear days during periods of light winds. Color-filled regions indicate data within one standard deviation of the mean. The asterisks indicate data points that exceeded one standard deviation from the mean (before they were excluded) and were thus excluded from subsequent analysis.



1
2 Figure 4: Linear regressions for data in Fig. 3 with the same color for each data set. R² values were 0.98 (blue), 0.98 (black) and
3 0.99 (red).



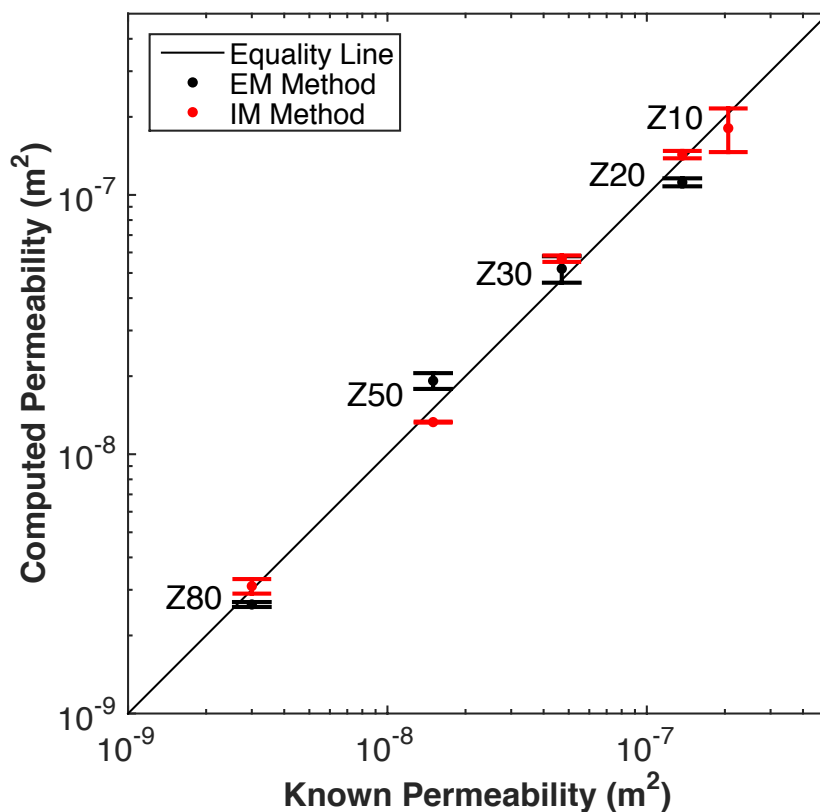
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4 Figure 5: Flow-through permeability as a function of relative flow resistivity using the M52 method and Eq. (9) at 50 Hz, 100 Hz
5 and 250 Hz. Three data points were acquired at each frequency and each foam type. The dashed red line defines a 2nd order
6 polynomial curve fit for the measurements with $p = 10^{(0.16 (\log \sigma)^2 - 0.14 (\log \sigma) - 8.59)}$.



1
2 Figure 6: Comparing flow-through (known) permeability with the EM method at 500 Hz and the IM method at 50 Hz for foam
3 samples given in Table 1. Z10 permeability was not computed by the EM method because k/σ_{pe} is nonlinear at high permeability,
4 as shown in Fig 3. For both methods, the value for each permeability measurement is given from the curve fit for that method and
5 the standard deviation is given from the original measurements.

6