



1 **Geoelectric monitoring at the Boulder magnetic observatory**

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3 Cletus C. Blum¹, Timothy C. White¹, Edward A. Sauter¹, Duff C. Stewart¹, Paul A. Bedrosian²,
4 Jeffrey J. Love¹

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6 ¹U.S. Geological Survey, Geomagnetism Program,
7 Box 25046 MS 966 DFC, Denver, Colorado 80225, USA

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9 ²U.S. Geological Survey, Crustal Geophysics and Geochemistry Science Center
10 Box 25046 MS 964 DFC, Denver, Colorado 80225, USA

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13

14 **Abstract**

15

16 Despite its importance to a range of applied and fundamental studies, and obvious parallels to a
17 robust network of magnetic-field observatories, long-term geoelectric field monitoring is rarely
18 carried out. The installation of a new geoelectric monitoring system at the Boulder Magnetic
19 observatory of the U.S. Geological Survey is summarized. Data from the system are expected,
20 among other things, to be used for testing and validating algorithms for mapping North American
21 geoelectric fields. An example time series of recorded electric and magnetic fields during a
22 modest magnetic storm is presented. Based upon our experience, we additionally present
23 operational aspects of a successful geoelectric field monitoring system.

24

25 **Introduction**

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27 Geoelectric fields are induced in the Earth's electrically conducting interior by time-dependent
28 geomagnetic field variation sustained by dynamic processes operating in the ionosphere and
29 magnetosphere. This induction occurs all the time, during both magnetically calm and stormy
30 conditions. During intense storms, induced geoelectric fields can drive quasi-direct currents in
31 bulk electric-power grids of sufficient strength to interfere with their operation, sometimes even
32 causing blackouts and damaging transformers [e.g. Boteler et al., 1998; Piccinelli and
33 Krausmann, 2014]. Notably, the magnetic storm of March 1989 [e.g. Allen et al., 1989] caused
34 the collapse of the Hydro-Québec power-grid system in Canada, leaving 6 million people without
35 electricity [Bolduc, 2002; Béland and Small, 2005]. More recently, the Halloween storm of
36 October 2003 caused operational failures in parts of the Swedish power-grid system [Pulkkinen et
37 al., 2005]. Some scenario analyses anticipate that the future occurrence of a rare but extremely
38 intense magnetic superstorm could cause widespread and long-lasting loss of electric-power [e.g.
39 Kappenman 2012] and entail substantial economic cost [e.g. Baker et al., 2008].

40

41 In support of a project for modeling and evaluating geoelectric hazards [e.g. Thomson, 2007;
42 Love et al. 2014], in June of 2016, the Geomagnetism Program of the U.S. Geological Survey
43 (USGS) commenced long-term geoelectric field monitoring at its Boulder, Colorado magnetic
44 observatory. The Boulder geoelectric monitoring project partially fulfills a directive in the United



45 States National Space Weather Action Plan [NSTC, 2015, Goal 5.5.4] (one of many given to
46 different agencies) for the Department of Interior to “assess and pilot a geoelectric monitoring
47 capability.” It is further consistent with strategic goals of the USGS Hazard Mission for
48 enhancing observations, pursuing fundamental understanding, and improving hazard assessments
49 [Holmes et al. 2013, Goal 1]. Geoelectric field monitoring is a natural extension of the
50 geomagnetic monitoring that is already the responsibility of the USGS Geomagnetism Program
51 [Love & Finn, 2011], and it is similar to long-term geoelectric monitoring projects supported in
52 other countries, including Great Britain [Kelly et al., 2013] and Japan [Fujii et al., 2015] and to
53 shorter-term campaign-style measurements common to magnetotelluric surveys [e.g. Ferguson,
54 2012]. From 1932 to 1942, analog geoelectric measurements were supported at the Tucson
55 magnetic observatory [Rooney, 1949]; from 1988 to 1995, geoelectric monitoring was performed
56 in Parkfield California as a part of an earthquake research project [Park, 1997]; otherwise, there
57 has been very little multi-year geoelectric monitoring carried out in the United.

58

59 **The Boulder site**

60

61 The Boulder magnetic observatory facility [Love et. al., 2015] is located on a flat-top butte, north
62 of the city of Boulder, Colorado, and east of the United States Rocky Mountains. The land is
63 rocky and sandy, sparsely covered with grass and cacti. The climate is semi-arid; summers are hot
64 ($>30^{\circ}$ C is common) with occasional thunderstorms; winters are cold (often $<-5^{\circ}$ C) with
65 occasional snowfall. The Boulder observatory is one of 14 supported by the USGS
66 Geomagnetism Program, and it is part of the International Real-time Magnetic Observatory
67 Network [www.intermagnet.org, Love and Chulliat 2013]. The observatory is also used by
68 Geomagnetism Program engineers and technical staff to develop and test new sensors, acquisition
69 systems, and operational procedures. The geoelectric monitoring system described herein are
70 located southwest of the observatory’s office building and primary geomagnetic monitoring
71 systems; see Figure 1.

72

73 **Electrodes and their installation**

74

75 Geoelectric data are obtained by measuring the voltage between pairs of non-polarizable
76 electrodes over time. For geoelectric monitoring at Boulder, Borin Stelth@ 2 Silver-Silver
77 Chloride (Ag-AgCl) electrodes were selected for their thermal stability, low noise characteristics,
78 long expected service life (>30 years), and relatively large surface area (200 cm^2); see Figure 2.
79 Electrode noise levels have been estimated to be significantly less than 1 mV based upon long-
80 term measurements of electrode potential in a temperature and salinity-controlled tank. In June of
81 2016, six electrodes were installed: two located near the data acquisition system, and one each
82 located 100 and 200 meters to the west and south from there. The electrodes were buried to
83 reduce grounding changes caused by time variation in soil moisture content and temperature that
84 can impart unwanted types of voltage variation. As shown schematically in Figure 3, at each
85 electrode location, a 1-m deep hole was dug; this was then partially filled with a thick layer of
86 bentonite clay, a substance that is very absorbant and commonly used as a ground-water barrier.
87 A 20-cm diameter, 1.25-m long, open-ended, polyvinyl chloride (PVC) pipe was placed vertically
88 in the hole and in contact with the bentonite; an electrode was placed in the bottom of the tube



89 with connecting wires leading out the top end. The tube was then partially filled with additional
90 bentonite until the electrode was covered; the rest of the tube was backfilled with sand; the space
91 around the outside PVC tube was filled with native rock and sand. The electrodes are connected
92 to the acquisition system using shielded coaxial cables further protected by PVC conduit. Two
93 electrodes are located near the acquisition system; one is used for the 100-m dipoles and the other
94 is used for 200-m dipoles; additional empty PVC pipes were installed in parallel for possible
95 future electrode emplacement that might be needed for testing and to provide redundancy.
96 Contact resistances between each pair of electrodes range from 200-300 Ω .

97

98 **Data acquisition and management**

99

100 Electrode voltage measurements are acquired using the Observation Reconfigurable Input and
101 Output System (ObsRIO) that USGS engineers developed in-house using the CompactRIO
102 (cRIO) hardware platform manufactured by National Instruments Corporation; the system is solar
103 powered; see Figure 4. The two standard data types acquired by ObsRIO are discrete 10 Hz
104 values and discrete 1-sec values. Ten hertz data values are formed from 100 Hz analog- and
105 digitally-filtered data, and the 1 second values are formed from the 10 Hz values. This data
106 construction process effectively eliminates aliasing from geoelectric variation with periods of less
107 than 0.1-sec (frequencies greater 10 Hz), but, otherwise, the 0.1-sec and 1 sec values are not
108 processed in any way. Data from the Boulder ObsRIO systems are transmitted to the USGS
109 database system, EdgeCWB [Patton et al., 2015], in Golden, Colorado via internet protocols in
110 near-real-time. Geomagnetism Program personnel make regular checks of the Boulder geoelectric
111 data to guard against artificial interference and to ensure continuity of operations.

112

113 **Example data**

114

115 In Figure 5 we show three days of Boulder geomagnetic and geoelectric data recording a
116 geomagnetic storm that occurred in October 2016. In global terms, the storm attained a maximum
117 $Dst = -104$ nT; maximum $Kp = 6$. Local to Boulder, however, the east geomagnetic component
118 saw a very abrupt and high amplitude signal (~ 150 nT), which induced a large geoelectric signal
119 in the north geoelectric component. The lowest frequency (diurnal) signals observed in the
120 geomagnetic time series are not reproduced in the geoelectric data due to a 30,000 second high-
121 pass analog filter within the acquisition system. All the measured geoelectric field variation is
122 well correlated with geomagnetic variation and is consistent with induction in the solid-earth.
123 Note, furthermore, that the consistency between the geoelectric time series for the 100 and 200-m
124 dipoles.

125

126 **Using the data**

127

128 A high priority for monitoring and assessing geoelectric hazards is the development of
129 capabilities for making maps of the geoelectric field, especially in real-time [e.g. NSTC, 2015,
130 Action 5.5.6]. One approach to regional and continental-scale geoelectric field mapping is
131 convolving maps of Earth impedance with maps of geomagnetic activity [e.g. Thomson, 2007;
132 Love et al. 2014]. Toward this end, long-term surface geoelectric field data, spanning both quiet



133 and storm times, are critical to validating predicted field data and to benchmarking different
134 modeling approaches [e.g. Kelbert et al. 2017; Bonner and Schultz 2017]. Additionally, surface
135 impedance functions can be calculated from synchronous electric and magnetic time series, as is
136 commonly done with magnetotelluric survey data. Long-term (months to years) geoelectric time
137 series data, as described here, constrain estimates of surface impedance to longer periods than
138 traditional magnetotelluric studies, facilitating investigations into deep-earth conductivity
139 structure. Finally, continuous recording of geoelectric and geomagnetic time series data,
140 particularly at sampling frequencies sufficient to capture the magnetotelluric ‘dead-band’ (10-0.1
141 Hz), can serve as remote-reference data for regional magnetotelluric surveys [Gamble et al. 1979;
142 Egbert 1997]. The availability of such data in near-real-time can reduce the logistical and cost
143 overhead associated with such surveys and increase data quality.

144

145 **Operational aspects of long-term electric field monitoring**

146

147 Long term electric-field monitoring introduces technical challenges that are distinct from
148 traditional magnetotelluric campaign or array deployments. As with other monitoring studies,
149 power supply, telemetry and system reliability are important design considerations for a
150 successful electric-field monitoring system. Furthermore, long-term electrode deployment adds
151 additional critical design elements, including thermal stability, moisture stability and lightning
152 suppression. We describe below aspects of the Boulder installation that we consider important to
153 achieving continuous, stable, low-noise geoelectric field data.

154

155 Long-term electric-field measurements are critically dependent upon the use of stable, low-noise
156 non-polarizable electrodes. A variety of electrode chemistries exist, with Ag-AgCl and Pb-PbCl₂
157 being two of the more commonly used types. Both of these electrode types are known for their
158 low noise levels, small thermal coefficients, and long-term stability (Petiau, 2000; Clerc et al.,
159 1998). The earth environment in which the electrodes are placed is additionally important. In
160 particular, greater thermal and moisture stability reduces non-inductive signals (e.g. diurnal
161 signals due to surface temperature variations). Toward this end, the USGS electrodes are buried 1
162 meter deep. Electrode noise further scales with the contact resistance between the electrode and
163 the earth. To minimize both, the earth within an area of 0.5 m² was removed and replaced with an
164 electrically-conductive bentonite slurry. A 1.25-m long, (1.0-m below ground) PVC tube was
165 emplaced into the bentonite to facilitate the installation and, if necessary, replacement of the
166 electrodes. The electrodes were placed into the bentonite slurry, covered with an additional layer
167 of bentonite, and the remainder of the PVC tube was filled with sand. Caps were subsequently
168 installed to seal the tube and prevent loss of moisture. To provide additional reliability and
169 redundancy, a network of electrodes were installed at each location.

170

171 The electrodes are connected via coaxial cable to the data acquisition system. Coaxial cable is
172 selected to reduce the introduction of capacitive noise via the long cable length deployed for this
173 application. The cable shields are grounded near the data acquisition system but isolated at the
174 electrode ends to avoid creating ground loops through the shielding. The coaxial cable was
175 further installed in PVC conduit to protect the cables from damage due to wildlife. Strain relief
176 was added to the PVC conduit at 30 meters intervals to prevent damage to the conduit and cable



177 during seasonal thermal expansion and contraction.
178
179 Lightning suppression, attenuation and protection are of the utmost importance in collecting
180 continuous long-term geoelectric field data. On two separate occurrences, buildings at the
181 Boulder Magnetic Observatory (BOU) have been directly struck by lightning. Significant effort
182 must be made to protect recording systems from damage under such conditions. The USGS has
183 installed a significant grounding system at the data acquisition site, consisting of a large steel
184 ground rod driven 2.34 meters deep. The coaxial shields are all connected to this ground, which
185 provides an electrical path for lightning induced signals and other noise sources incident on the
186 shields. The electrodes are further connected to a pre-amplifier and lightning isolation circuit
187 board. The board was originally designed for the NIMS portable MT system, developed by
188 Narod Geophysics, LTD. There are two components of lightning protection integrated on this
189 board. First are a series of 75 V_{DC} spark gap devices, connected individually to each incoming
190 electrode connection. Additionally, varistors are used in a suppression mode to shunt excessive
191 currents incident on the incoming channels. This board has been used to collect hundreds of
192 thousands of hours of data for the EarthScope US Array program with very few cases of failure
193 from lightning.
194
195 Amplification and filtering can be an important component of electric-field monitoring depending
196 upon the application as well as the sensitivity and dynamic range of the data acquisition system.
197 Quiet-time electric-field amplitudes are on the order of 0.1mV/km or less; hence measured
198 voltages across electrode pairs separated by ~100 m may be on the order of 0.01 mV. Instrument
199 gain is commonly used to amplify the raw signals; the gain at the Boulder monitoring station is a
200 factor of 10. Filtering may also be beneficial to obtaining quality electric-field data. There are
201 two analog filters incorporated within the Boulder data acquisition system. A notch filter
202 attenuates 60 Hz signal, common to North America's power distribution network, by a factor of
203 at least 20 dB. An additional analog high-pass filter, with a time constant of roughly 10.5 hours,
204 can optionally be turned on. This filter may be used to attenuate long-period signals, including
205 diurnal signal arising from thermal fluctuations in the electrodes and long-term drift.
206
207 A low-noise, high input-impedance data acquisition system with moderately high sample rate is
208 needed for geoelectric field monitoring. To meet this need we developed the Observation
209 Reconfigurable Input and Output System (ObsRIO) based on the CompactRIO (cRIO) hardware
210 platform manufactured by National Instruments (NI). A key design aspect of the ObsRIO
211 platform is its modularity and ability to change configurations in response to rapidly changing
212 scientific needs. Minimal development time is required to create new images of ObsRIO for
213 different scientific applications. The USGS has, for example, designed a portable magnetotelluric
214 variant of the system which acquires both electric and magnetic field data and is battery powered.
215
216 The ObsRIO employs 4-channel simultaneous sampling on a 24-bit, +/-10 VDC (direct current
217 voltage) analog to digital converter (ADC, NI 9239). The ADC is configured to sample at a
218 frequency of 10 kHz. A box-car filter is used to decimate the data from 10 kHz to 1 kHz and
219 ultimately to separate 100 Hz, 10 Hz, and 1 Hz data output streams for logging and transmission.
220 A GPS clock was used to discipline the FPGA (field programmable gate array) clock, a process



221 where the GPS signal is used to constantly calibrate the FPGA clock. Timestamped samples are
222 passed into a FIFO for further processing, logging and transmission on the real-time controller for
223 the cRIO chassis. Pairing the ObsRIO system with a cellular device allows for real-time data
224 collection and transmission.

225

226 The data acquisition system was finally designed with automated switching power-source control.
227 ObsRIO automatically charges one battery, while powering the system from a separate battery
228 electrically isolated from the charging source. A series of programmable relays and low
229 resolution ADCs are used to set the power supply state for the system and switch charging and
230 load batteries as needed. This is an important aspect of the ObsRIO system, as noisy power
231 sources (such as solar) are kept from contaminating the desired geoelectric fields. This feature is
232 additionally critical to campaign style deployments, which rely upon batteries and solar power for
233 power.

234

235 **Disclaimer**

236

237 Any use of trade, firm, or product names is for descriptive purposes only and does not imply
238 endorsement by the U.S. Government.

239

240 **Acknowledgements**

241

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243 data can be viewed on the USGS geomagnetism plots page (<http://geomag.usgs.gov/plots/>) and
244 downloaded from (<http://dev-geomag.cr.usgs.gov/ws/edge/>). We thank T. Theissen from Borin
245 Manufacturing Inc. for providing the electrodes used at the Boulder magnetic observatory.

246

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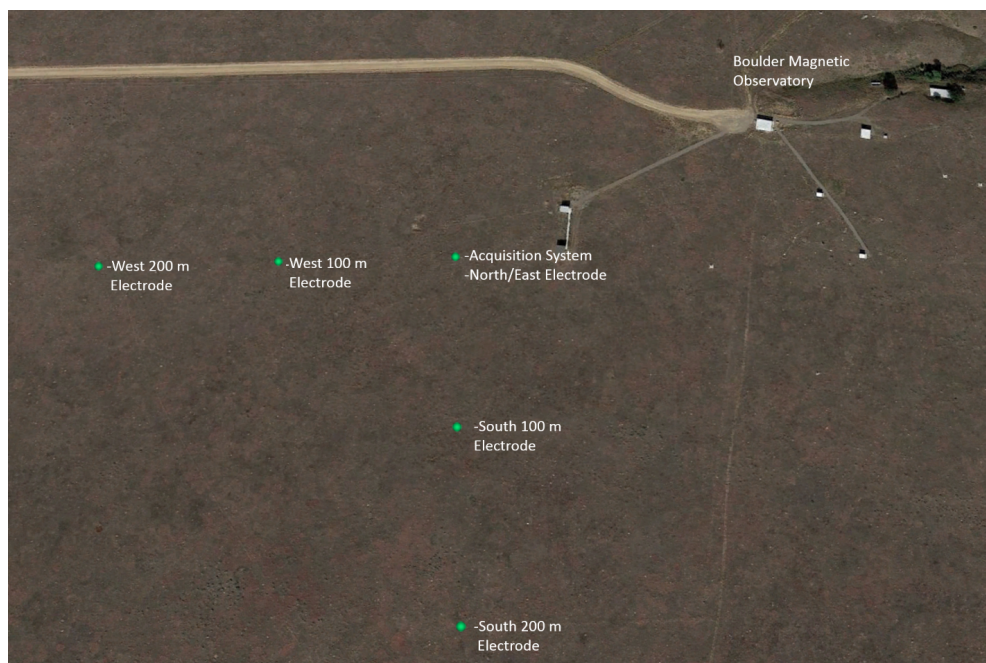


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338 **Figure captions**
339
340 **Figure 1:** Map of geoelectric-monitoring deployment at the Boulder observatory. North is up.
341
342 **Figure 2:** The Borin Stelth® electrodes used for geoelectric-monitoring at the Boulder
343 observatory.
344
345 **Figure 3:** Schematic of electrode installation.
346
347 **Figure 4:** Geoelectric field data acquisition system at the Boulder observatory. (a) View to the
348 northeast of the data acquisition system. Electric field lines, protected by PVC conduit, extend
349 west and south. (b) Interior view of data acquisition system in environmentally-sealed enclosures.
350 Electric, and optionally magnetic, inputs are brought into the right enclosure with shielding tied to
351 the observatory grounding system. The left enclosure contains the ObsRIO is in the upper left, the
352 switching power source controller on the right, and a cellular model in the center.



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Figure 5: Three days of geomagnetic and geoelectric field variation recorded at the Boulder observatory: (a) north (blue) and east (gray) geomagnetic components, (b) north geoelectric component, 100 (black) and 200 (red) dipole, (c) east geoelectric component, 100 (black) and 200 (red) dipole.



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Figure 1.



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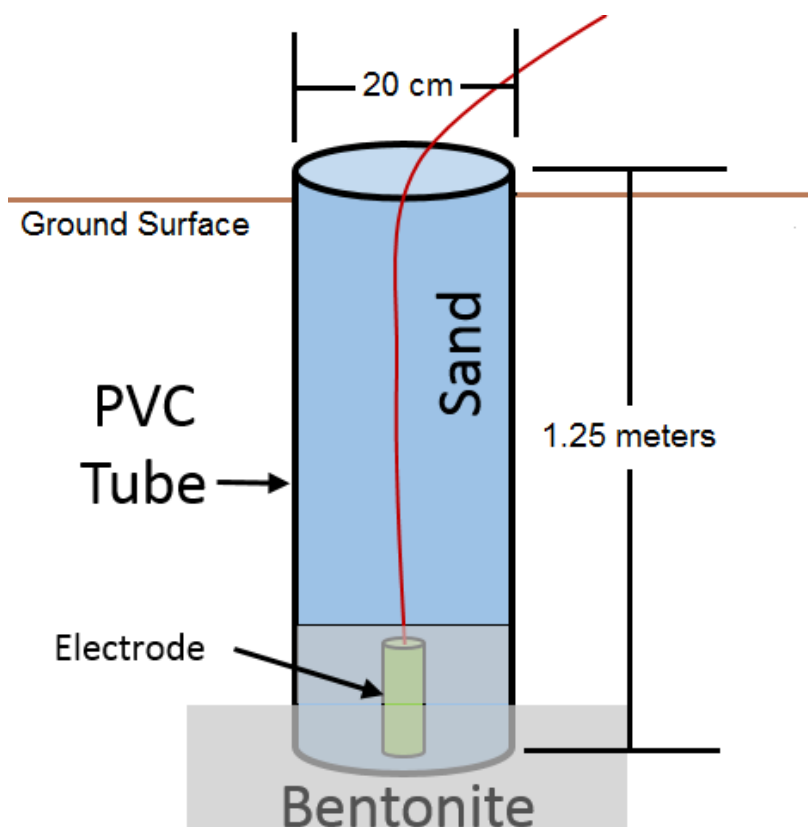


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Figure 2.



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Figure 3.

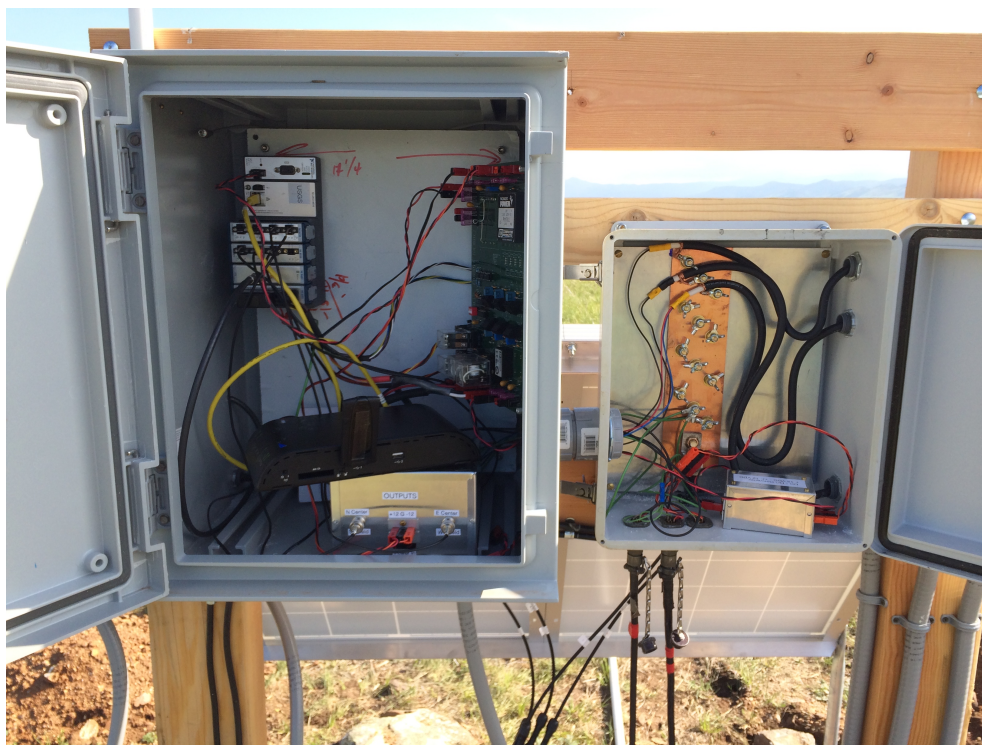


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Figure 4(a)



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Figure 4(b).

