

Response to reviewers' comments

First of all, we would like to thank the reviewers for their helpful comments. In this document, the reviewers' comments are given in boldface and our answers are in normal type. Line and section numbers refer to the original manuscript.

Reviewer #1

Major remarks:

Comment 1: For such a serious problem as space magnetic field measurements the MS contains non-metrological definitions as “approximately”, “slightly over” etc. at estimation of physical values and approximation procedures. See, for example:

1. **p. 4, lines 15-16: “... the spin axis is assumed to be approximately aligned with the $P_z = S_3$ axis” [The admissible errors should be estimated.]**
2. **p. 6, lines 10-15, Eqs. (11)-(15). [The admissible approximation errors should be estimated.]**
3. **p. 7, line 11: “... and further dropping second order factors, “ [The approximation errors should be indicated.]**
4. **p. 11, line 1: “... slightly over and under the spin frequency: ... with ... and slightly over/under n ...” [The admissible intervals should be estimated.]**
5. **p. 11, line 20: “... slightly over/under n.” [The admissible intervals should be estimated.]**
6. **p. 11, line 28: “... can be omitted due to linearization.” [The approximation errors should be indicated.]**
7. **p. 11, line 32: “... if the initial set of calibration parameters is not too inaccurate.” [The admissible approximation errors should be indicated.]**
8. **[During linearization procedure (see, for example, p.6, lines 10-15; p.11, line 28) the basic equations are simplified what leads to the appearance of additional errors at data processing. So, the errors of such an approximation should be estimated, at least for main cases.]**

Points 1, 2, 3, 6, 7, and 8 deal with errors associated to the linearization procedure and/or in the corresponding assumptions regarding the calibration parameters. The aim of the linearization procedure is to obtain the uncertainties $\Delta\sigma_{P_x/y}$, Δg , $\Delta\phi_{S12}$, $\Delta O_{S1/2}$, and $\Delta\theta_{S1/2}$ in calibration parameter determination under different conditions, shown in the right column of Table 2. The actual calibration parameter estimates, however, are unaffected by these errors, as they are obtained by using the full – not linearized – calibration Equation (9), with matrices (4) to (7). The question is, hence, how much the parameters g , G_p , G_a , σ_{P_x} , σ_{P_y} , $\delta\theta_{S1}$, $\delta\theta_{S2}$, $\delta\phi_{S12}$ may deviate from the assumed values (see Equations 11 to 15) until the errors in the uncertainties $\Delta\sigma_{P_x/y}$, Δg , $\Delta\phi_{S12}$, $\Delta O_{S1/2}$, and $\Delta\theta_{S1/2}$ in Table 2 become unacceptably large.

As shown in the application section 6, we are only interested in the orders of magnitude of the uncertainties (a factor of 10). Conservatively limiting the error to a factor of 2, and taking into account that relative errors from individual matrices (16) to (19) may increase by multiplication due to Equation (10), we obtain individual limits on the relative deviations D of the parameters of: $2 = D^4$, $D = 1.189$, i.e., 19%.

Such an error is extraordinarily large when compared to the accuracy in the knowledge of the calibration parameters and of the geometry of the spacecraft, even before performing any in-flight calibration. For the angles σ_{P_x} , σ_{P_y} , $\delta\theta_{S1}$, $\delta\theta_{S2}$, and $\delta\phi_{S12}$, this means deviations from 0 by up to 11° are

acceptable ($\arcsin(19\%)$). Note that alignment uncertainties should usually be lower than 1° . For the gains g , G_p , and G_a , errors of 19% would be theoretically acceptable. Ground calibration, however, should reduce these errors to less than 0.1%. Hence, the assumptions made due to linearization (e.g., Equations 11 to 15) are not restrictive at all, and easily fulfilled in practice.

Points 4 and 5 deal with estimating amplitudes of natural magnetic field fluctuations in the vicinity of the spin frequency or second harmonic. Slightly over/under n transforms into frequencies that are “slightly” over or under the first/second harmonic frequency. The question is how large “slightly” needs to be. It should be large enough so that an increased amplitude at the spin frequency or second harmonic does not leak significantly into the selected frequency bins. It should also be small enough so that the amplitudes determined at the selected frequencies resemble the natural amplitude level at the spin frequency or second harmonic.

The ratio of spin tone leakage with respect to natural fluctuations around the spin frequency is a function of spin tone amplitude and the Fourier transform window. Choosing the optimal frequencies above and below ω would require a recalculation for each subinterval considered. In practice, experience from THEMIS and MMS calibration activities shows that frequencies 15% of ω above and below ω and 2ω are a good choice. The reason is that $\pm 15\%$ of ω is a large “distance” in frequency with respect to the sharp spin tone signatures from incorrect calibration parameter choice and leakage, yet $15\% \omega$ is still a small frequency interval for natural fluctuations. These relative frequencies have also been used in the THEMIS example presented in section 6.

We opted for including a general discussion on admissible errors between sections 6 and 7 (new section 7). A discussion on choices in frequency above/below ω is added in page 11, line 5, after Equations (30) and (31).

Comment 2: P. 11, lines 6-9. It is unclear, how to de-trend the B data, i. e. to separate the studied process and linear trend with given error.

The Fourier transform is applied either to the spin axis component data or to the modulus of the spin plane field. That component/modulus is detrended by simply subtracting a linear fit to it, as we now state in the paper.

Comment 3: P. 13, line 8. What does it mean “... as temperatures relax to stationary values.” in practical sense, i. e. admissible unbalance between stationary value and real unsteady temperature after eclipse, for example? What level was assumed by authors during data processing? It should be clearly indicated.

The admissible unbalance is very spacecraft and instrument specific. Some instruments/spacecraft show significant changes in magnetometer calibration parameters with just a few degrees change in sensor/electronics/spacecraft temperatures. At other spacecraft, almost no changes are apparent, although temperatures vary by several tens of degrees. During processing of the THEMIS spacecraft data we excluded eclipse and high field magnetometer saturation intervals. During the remaining time intervals, the electronics and sensor temperatures vary within 3 degrees, which in the THEMIS case is totally insignificant for the calibration parameters. We state this now at the end of page 14.

Comment 4: P. 10, line 27. Why for B_p "... the minimal modulus of the spin plane field over the subinterval: $\min(p(B_x^2 + B_y^2))$." was chosen? It seems to be the better value is $\text{avg}(p(B_x^2 + B_y^2))$.

Numerical example: $G_p = 0.999$, $G_a = 1.0001$, $g = 1.002$, $\theta_{S1} = \pi/2 + 0.001$, $\theta_{S2} = \pi/2 - 0.0015$, $\phi_{S12} = \pi/2 + 0.002$, $\sigma_{Px} = 0.0008$, $\sigma_{Py} = -0.0012$. Normalized magnetic field in the non-spinning (inertial), orthogonal, spin-axis aligned ($Z = z$) coordinate system: $B_X = 0.3$, $B_Y = 0.8$, $B_Z = -0.5196$. Spin frequency is 2π . The test data was generated for 5 rotation periods with the time discretization $dt = 0.2$. True value $B_p = \sqrt{B_x^2 + B_y^2} = 0,85440$. The estimation of B_p using the minimum of the modulus of the B' projection on plane XOY (the rotation plane) gives the value $dB_{p_min} = B_p - \min(\sqrt{B_x'^2(t) + B_y'^2(t)}) = 0,00236270$. The estimation of B_p at use of the average value of the modulus for the B' projection on plane XOY gives the value $dB_{p_avg} = B_p - \text{avg}(\sqrt{B_x'^2(t) + B_y'^2(t)}) = 0,00087464$. Finally $(dB_{p_min})/(dB_{p_avg}) = 2.7013$.

We agree that the slightly better value is $\text{avg}(\sqrt{B_x^2 + B_y^2})$. However, dB_{p_avg} and dB_{p_min} are both very small in comparison to B_p , which is the quantity we are interested in here, and we considered $\min(\sqrt{B_x^2 + B_y^2})$ to be the more conservative choice, as stated in the paper.

Minor remarks:

Comment 6: P.5, line 16, Eq. (6): No definition of angle 'a.

As stated in the sentence above the equation, ϕ_a is a rotation angle about the spin axis.

Comment 7: P.9, Table 2, group 1: No definition of F_a .

Comment 8: P.9, line 20, p.10, line 26: No definition of F_a .

The definition is stated on page 9 line 19. F_a is then exactly defined in Equation (31).

Comment 9: P.9, Table 2, group 3: it should be OS1 and OS2 instead of OS1 and OS1.

Comment 10: P.10, line 12: it should be $GT(T_s, T_e)$ instead of $GT(T_s, T_s)$.

Thank you very much for pointing out these typos. They are now corrected.

Comment 11: P.13, line 16: it should be FGM instead of FGL.

In this case, FGL is correct. It is the name of the data product and not the acronym for Fluxgate Magnetometer, the instrument.

Reviewer #2

Comment 12: Equations (20,21)

Although it is entirely obvious that (ωt) is the spin parameter, to be consistent with the excellent presentation of parameter definitions up to this point, (ωt) could beneficially be defined here. As the paper is written this spin parameter appears to apply to both steps 1 and 4, the

amplitude modulations and demodulations. In the case that the modulation frequencies are identical the situation can be called synchronous demodulation, which has huge advantages. In general though, the modulation and demodulation frequencies are not identical, but are determined and matched very accurately. As the spacecraft ages and fuel is used, not only are spin angles changing, but so are moments of inertia. The spin frequency cannot be determined from the short analysis periods, due to well understood uncertainty principles. As noted earlier in the paper the spin frequency/angle were determined as a priors, using the IGRF and other tools. Some brief discussion is recommended as to the definition of omega and (ωt), and how they relate to the amplitude demodulation parameters.

Thank you for the suggestion. We now define ωt right after Equations (20) to (22).

The spin rate is not usually determined from magnetic field measurements, but from independent sun sensor or star tracker measurements. Hence, the spin rate is adjusted regularly and is known with very high accuracy. Exact knowledge of this frequency is highly important for spin demodulation, which is done in a later part of instrument data processing. However, the estimate of the calibration parameters does not rely on exact demodulation, but only on the amplitude of certain frequencies within the Fourier transformed signal. Small shifts below the frequency resolution of the DFT will therefore only result in a slightly smaller sensitivity, as the amplitude of the considered frequency is reduced by a small amount.

Comment 13: Also, for the determination of g, the X/Y gain ratio, the choices of +/-15% [page 15] of the carrier/spin frequency seem large in context of equations 30 and 31. Is this a requirement of the data rate?

See answer to comment 1, points 4 and 5: The large separations between frequencies are there to avoid significant leakage from the signals at ω and $2*\omega$.

Comment 14: Equations (24,25)

Each of these equations consists of five terms, pair-wise similar. As this is the end of section 3, for the general reader some brief summary descriptions could be useful. The first terms are the primary measurement terms, while the second and third terms represent (roughly) the modulations of the X/Y offsets and the projection from the spin axis into the spin tone. The fourth and fifth terms are the 2nd harmonic terms resulting mainly from the differential gains of the X/Y channels. A quick review of the physical mechanism leading to a detectable 2nd harmonic term would be useful as the reader at this point needs a clear understanding that he or she is considering only despun data. Section 4 goes into all of this in further detail.

As suggested, we have added a discussion on Equations (24) to (26) at the end of section 3.

Comment 15: The use of rotations in fields as the basis for a calibration methodology now has a long history. This reader's first contact with such ideas was that of A.W. Green Jr, in the 1980's. Green took on the much easier task of calibrating observatory magnetometers, for which multiple rotation axes were possible. Green's description of his method can be found as [doi.org/10.1016/0031-9201\(90\)90217-L](https://doi.org/10.1016/0031-9201(90)90217-L) . Such methods have come a long way.

Thank you very much for making us aware of this reference. We cite it now in the introduction.

Advanced calibration of magnetometers on spin-stabilized spacecraft based on parameter decoupling

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Abstract. Magnetometers are key instruments onboard spacecraft that probe the plasma environments of planets and other solar system bodies. The linear conversion of raw magnetometer outputs to fully calibrated magnetic field measurements requires the accurate knowledge of 12 calibration parameters: 6 angles, 3 gain factors, and 3 offset values. The in-flight determination of 8 of those 12 parameters is enormously supported if the spacecraft is spin stabilized, as an incorrect choice of those parameters will lead to systematic spin harmonic disturbances in the calibrated data. We show that published equations and algorithms for the determination of the 8 spin-related parameters are far from optimal, as they do not take into account the physical behavior of science-grade magnetometers and the influence of a varying spacecraft attitude on the in-flight calibration process. Here, we address these issues. Based on decades-long developments and experience in calibration activities at the Braunschweig University of Technology, we introduce advanced calibration equations, parameters, and algorithms. With their help, it is possible to decouple different effects on the calibration parameters, originating from the spacecraft or the magnetometer itself. A key point of the algorithms is the bulk determination of parameters and associated uncertainties. Lowest uncertainties are expected under parameter specific conditions. By application to THEMIS-C magnetometer measurements, we show where these conditions are fulfilled along a highly elliptical orbit around Earth.

1 Introduction

The investigation of the plasma environment in the heliosphere, around planets, moons, comets, or other solar system bodies, requires accurate in-situ observations of the magnetic field. Magnetometers on board spacecraft can provide these key measurements if accurately calibrated on ground and in flight. The calibration process delivers the parameters needed to convert raw magnetometer measurements into magnetic field observations $\mathbf{B} = (B_x, B_y, B_z)^T$ in physically meaningful coordinate systems and units (usually nanotesla: nT). Commonly, a linear calibration equation is applied for this conversion (e.g., Fornaçon et al., 1999; Balogh et al., 2001b; Auster et al., 2008):

$$\mathbf{B} = \mathbf{C} \cdot (\mathbf{B}_S - \mathbf{O}_S) \quad (1)$$

Here $\mathbf{B}_S = (B_{S1}, B_{S2}, B_{S3})^T$ is the raw magnetometer output in non-orthogonal sensor coordinates, \mathbf{O}_S corrects for non-vanishing magnetometers outputs in zero ambient fields (so-called offsets, which include spacecraft-generated magnetic fields

at the sensor position), and \mathbf{C} is the 3×3 coupling matrix. This matrix may have the following form (e.g., Kepko et al., 1996):

$$\mathbf{C} = \begin{pmatrix} \sin \theta_1 \cos \phi_1 & \sin \theta_1 \sin \phi_1 & \cos \theta_1 \\ \sin \theta_2 \cos \phi_2 & \sin \theta_2 \sin \phi_2 & \cos \theta_2 \\ \sin \theta_3 \cos \phi_3 & \sin \theta_3 \sin \phi_3 & \cos \theta_3 \end{pmatrix}^{-1} \cdot \begin{pmatrix} G_{S1} & 0 & 0 \\ 0 & G_{S2} & 0 \\ 0 & 0 & G_{S3} \end{pmatrix} \quad (2)$$

The coupling matrix \mathbf{C} depends on three scaling factors (G_{S1} , G_{S2} , and G_{S3} , also called the gains) and six angles (θ_1 , θ_2 , θ_3 , and ϕ_1 , ϕ_2 , ϕ_3) which define the directions of the three sensor axes in the orthogonal coordinate system to which \mathbf{B} pertains.

- 5 Calibrating a magnetometer means finding the three gains, six angles, and three offset components (i.e., in total 12 parameters) so that \mathbf{B} can accurately be obtained from \mathbf{B}_S .

Ground calibration of magnetometers is facilitated by rotating them in Earth's magnetic field (Green, 1990). Similarly, operating a magnetometer on a spinning spacecraft, instead of on a three-axis stabilized spacecraft, enormously supports the in-flight determination of 8 of the 12 calibration parameters. These 8 spin-related parameters are: the two spin plane offset components, five of the six sensor direction angles (all but one defining the rotation about the spin axis), and the ratio of the spin plane gains. The reason is that an incorrect choice in any of those 8 spin-related parameters leads to the appearance of clear, systematic signals at the spin frequency (also called the first harmonic) and/or at twice the spin frequency (second harmonic) in the de-spin magnetic field measurements. Hence, minimization of these signals can be used to determine the 8 calibration parameters, as described in Farrell et al. (1995) and Kepko et al. (1996).

- 10 The other 4 (spin-unrelated) parameters are the absolute gains in the spin plane and along the spin axis, the spin axis offset, and the angle of rotation of the sensor about the spin axis. Gains and angle can be derived in flight by comparison of magnetic field measurements with the International Geomagnetic Reference Field (IGRF) or the Tsyganenko field models, which are fairly accurate close to Earth (e.g., Thébaud et al., 2015; Tsyganenko and Sitnov, 2007). For the determination of the spin axis offset in flight, a list of different methods exists. Typically, the offset is obtained from careful analysis of Alfvénic magnetic field fluctuations, present in the pristine solar wind (e.g., Belcher, 1973; Hedgecock, 1975; Leinweber et al., 2008). If strongly compressional fluctuations are observed instead of Alfvénic fluctuations, then the mirror mode method may be used (Plaschke and Narita, 2016; Plaschke et al., 2017). The offset may also be obtained from comparison with measurements from an absolute magnetometer or time-of-flight measurements of electrons emitted and observed by an electron drift instrument (Georgescu et al., 2006; Nakamura et al., 2014; Plaschke et al., 2014). Furthermore, the spin axis offset may also be obtained in regions of space where the fields are known, for instance, in diamagnetic cavities in the vicinity of comets (Goetz et al., 2016a, b).

- From the preceding paragraphs, the reader might get the impression that in-flight calibration of magnetometers on spinning spacecraft is a solved issue; and in theory this is the case. However, as we will show in the following sections, the published methods for spin-aided calibration (Farrell et al., 1995; Kepko et al., 1996) are not optimal in practice because they do not take into account the physical behavior of the sensor package and the influence of a varying spacecraft attitude on the in-flight calibration.

This paper aims at identifying deficiencies and suggesting improvements with respect to the calibration Equations (1) and (2) and the specific choice of the calibration parameters. Thereafter, we identify optimal conditions for spin-related calibration parameter determination. Finally, we introduce advanced algorithms for parameter determination based on our findings, that

Table 1. List of coordinate system notations used in this paper. After Table 1 in Kepko et al. (1996).

notation	characteristics
S1, S2, S3	spinning, non-orthogonal, sensor axes aligned
Px, Py, Pz	spinning, orthogonal, sensor package system ($Pz = S3$)
x, y, z	spinning, orthogonal, spin-axis aligned (z -axis)
X, Y, Z	non-spinning (inertial), orthogonal, spin-axis aligned ($Z = z$)
X', Y', Z'	despun non-orthogonal coordinate system

lend itself for automation and distribution of calibration activities. A version of these algorithms is routinely applied to calibrate magnetometer data from the Magnetospheric Multiscale (MMS) mission (Burch et al., 2016; Torbert et al., 2016; Russell et al., 2016). The calibration principles and algorithms described here are based on developments at the Braunschweig University of Technology (Fornaçon et al., 2011) that have been successfully applied for decades to calibrate magnetometer data from, e.g.,
5 the Equator-S (Fornaçon et al., 1999), the Cluster (Balogh et al., 2001a, b), and the Time History of Events and Macroscale Interactions during Substorms (THEMIS) missions (Angelopoulos, 2008; Auster et al., 2008).

2 Calibration Equation and Parameters

Equations (1) and (2) in principle allow for any linear conversion of \mathbf{B}_S into \mathbf{B} . The coupling matrix (2) is obviously split into two components:

$$10 \quad \mathbf{C} = \mathbf{\Theta} \cdot \mathbf{G} \quad (3)$$

Here, the diagonal matrix \mathbf{G} includes only the gains, and the matrix $\mathbf{\Theta}$ includes only the angular dependencies. Let's focus first on the matrix $\mathbf{\Theta}$. The parameters θ_1 , θ_2 , and θ_3 are the angles between the three mutually non-orthogonal sensor axes (directions S1, S2, and S3) and the spin axis in z -direction in an orthogonal, spin axis aligned and spacecraft fixed coordinate system (directions x , y , and z). The parameters ϕ_1 , ϕ_2 , and ϕ_3 correspond to the angles between the spacecraft fixed x -direction
15 in the spin plane (x - y -plane, perpendicular to the spin axis) and the projections of the sensor axes onto that plane. For simplicity, the sensor axes S1, S2, and S3 are assumed to be approximately aligned with x and y and z . Note that all coordinate systems used in this paper are listed in Table 1.

The individual link of the sensor axes to a spacecraft fixed, spin axis aligned system is an issue here, as it does not reflect the actual situation on the spacecraft: There, the three sensor axes are typically packaged together into one sensor system. One
20 of the design criteria of modern fluxgate magnetometer sensors is the temperature and long-term stability of the sensor axis directions as defined with respect to the sensor package. The angles between the sensor axes are usually well-known from ground calibration activities (e.g., Auster et al., 2008; Russell et al., 2016), and we can expect the three angles between the sensor axes to be relatively stable parameters. Consequently, in a first step, the magnetometer output in non-orthogonal sensor coordinates should be transformed into an orthogonal sensor package fixed coordinate system (coordinates: Px, Py, Pz , see

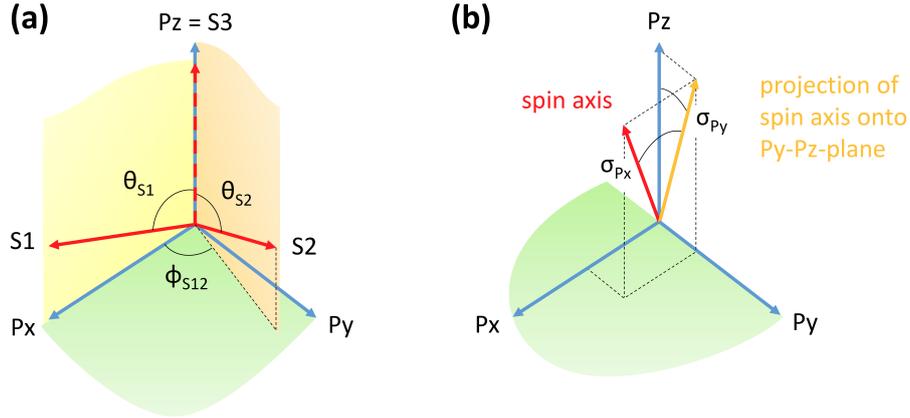


Figure 1. Sketch of the coordinate systems: (a) sensor axes in the sensor package coordinate system, (b) spin axis and rotation angles σ_{Px} and σ_{Py} in the sensor package coordinate system.

Table 1). The conversion matrix may have the following form:

$$\Gamma = \begin{pmatrix} \sin\theta_{S1} & 0 & \cos\theta_{S1} \\ \cos\phi_{S12}\sin\theta_{S2} & \sin\phi_{S12}\sin\theta_{S2} & \cos\theta_{S2} \\ 0 & 0 & 1 \end{pmatrix}^{-1} \quad (4)$$

Here, θ_{S1} and θ_{S2} are the angles between the sensor axes S1 and S2 with respect to $S3=Pz$, and ϕ_{S12} is the angle between the projections of S1 and S2 onto a plane perpendicular to S3, the Px - Py plane. Note that S1 lies in the Px - Pz plane (see Figure 5 1a).

In the next step, the orientation of that sensor package system needs to be defined in a spacecraft-fixed spin axis aligned coordinate system. This latter transformation is expected to change every time there is a maneuver of the spacecraft, as fuel consumption will change the tensor of inertia and, thus, the spin axis direction in any spacecraft fixed coordinate system. The spin axis direction can be defined in the orthogonal sensor package system using two parameters or angles. During maneuvers, only those two parameters/angles should change, because the geometry inside the sensor package should not be affected. A rotation matrix Σ into a spin axis aligned coordinate system dependent on the two angles σ_{Px} and σ_{Py} can be defined as follows:

$$\Sigma = \begin{pmatrix} \cos\sigma_{Px} & 0 & -\sin\sigma_{Px} \\ 0 & 1 & 0 \\ \sin\sigma_{Px} & 0 & \cos\sigma_{Px} \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\sigma_{Py} & -\sin\sigma_{Py} \\ 0 & \sin\sigma_{Py} & \cos\sigma_{Py} \end{pmatrix} \quad (5)$$

Here, σ_{Py} is the angle between Pz and the projection of the spin axis onto the Py - Pz -plane, positive towards Py ; σ_{Px} is the angle between that projection and the spin axis, positive towards Px . The angles are illustrated in Figure 1b. Note that the spin axis is assumed to be approximately aligned with the $Pz = S3$ axis. As a result, the angles σ_{Px} and σ_{Py} will be small and can be associated with the Px and Py coordinates of a unit vector that points in spin axis direction.

Using the angles σ_{P_x} and σ_{P_y} to define the spin axis direction is advantageous over using the angles θ_3 and ϕ_3 , as the latter angle is badly defined if θ_3 is small. Furthermore, it should also be noted that a change in direction of the spin axis requires an update of all angles of matrix Θ as defined above, even though the magnetometer (sensor) itself is unaffected. Only two parameters (σ_{P_x} and σ_{P_y}) need to be changed here to adapt the matrix Σ to the new spin axis direction.

- 5 To completely orient the sensor package (system) in the spin axis aligned coordinate system, a rotation about the spin axis (rotation matrix Φ) also needs to be taken into account:

$$\Phi = \begin{pmatrix} \cos \phi_a & -\sin \phi_a & 0 \\ \sin \phi_a & \cos \phi_a & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad (6)$$

As we will show later, this rotation does not affect the spin tone content in the despun magnetic field observations. The angle is affected by the orientation of a magnetometer boom and may change due to boom bending (Farrell et al., 1995).

- 10 Altogether, we can replace the orthogonalization and reorientation matrix Θ by $\Phi \cdot \Sigma \cdot \Gamma$ in Equation (3). Let's focus then again on the gain matrix \mathbf{G} in that equation. As mentioned in the introduction, the spacecraft spin aids the determination of the ratio $g^2 = G_{S1}/G_{S2}$ of the spin plane gains, but not the absolute gains in the spin plane $G_p = \sqrt{G_{S1}G_{S2}}$ and along the spin axis $G_a = G_{S3}$. Hence, it makes sense to use the parameters g and G_p instead of G_{S1} and G_{S2} in the matrix \mathbf{G} , to decouple parameters that can be frequently updated from parameters that are only obtainable in flight from comparison to model fields
- 15 or measurements of other instruments:

$$\mathbf{G} = \begin{pmatrix} gG_p & 0 & 0 \\ 0 & G_p/g & 0 \\ 0 & 0 & G_a \end{pmatrix} \quad (7)$$

Note that Kepko et al. (1996) use the difference of the inverse gains $\Delta G_{21} = 1/G_{S2} - 1/G_{S1}$ instead of g . However, later changes in the absolute gains G_{S1} and G_{S2} then require necessarily an update of ΔG_{21} in order to avoid perturbations at the second harmonic in the despun data. The gain ratio g , instead, is decoupled from changes in the absolute gains G_p and G_a .

- 20 The gains should be stable parameters in the absence of temperature variations. These variations in the gains can be determined from ground calibration, resulting in a diagonal gain correction matrix $\mathbf{G}_T(T_s, T_e)$ that is dependent on the magnetometer sensor (T_s) and electronics (T_e) temperatures. That matrix should be directly applied to the magnetometer output \mathbf{B}_S , requiring the knowledge of the sensor and electronics temperatures:

$$\mathbf{B}_{ST} = \mathbf{G}_T(T_s, T_e) \cdot \mathbf{B}_S \quad (8)$$

- 25 The resulting temperature corrected output \mathbf{B}_{ST} may then be further converted to \mathbf{B} via the coupling matrix $\mathbf{C} = \Phi \cdot \Sigma \cdot \Gamma \cdot \mathbf{G}$ and the offset vector \mathbf{O} using Equation (1), after replacing \mathbf{B}_S with \mathbf{B}_{ST} . This also has the advantage that the further applied absolute gains G_p and G_a and the gain ratio g^2 should all be approximately 1 and unitless.

Altogether, we suggest to use the following improved calibration equation:

$$\mathbf{B} = \Phi \cdot \Sigma \cdot \Gamma \cdot \mathbf{G} \cdot \underbrace{(\mathbf{G}_T(T_s, T_e) \cdot \mathbf{B}_S - \mathbf{O}_S)}_{=\mathbf{B}_{ST}} \quad (9)$$

with matrices defined in Equations (4) to (7) instead of the simpler Equations (1) and (2). The parameters whose determination is supported by the spacecraft spin are: θ_{S1} , θ_{S2} , ϕ_{S12} , σ_{Px} , σ_{Py} , g , O_{S1} , and O_{S2} .

3 Calibration Parameter Influence on Spin Tone Harmonics

To determine the influence of the calibration parameters on the spin tone harmonic disturbances in the despun magnetic field measurements, we use a similar mathematical approach to Kepko et al. (1996) in this section. Based on the results, we go on to derive the optimal conditions for the determination of each parameter in section 4.

First, we compute the temperature corrected sensor output B_{ST} as a function of the external field B in the spinning coordinate system:

$$B_{ST} = \mathbf{G}^{-1} \cdot \mathbf{\Gamma}^{-1} \cdot \mathbf{\Sigma}^{-1} \cdot \mathbf{\Phi}^{-1} \cdot B + O_S \quad (10)$$

10 We linearize all the matrices, using the following simplifying assumptions. The validity of these assumptions and the admissible deviations are discussed in section 7.

$$g \approx 1, \quad G_p \approx 1, \quad G_a \approx 1 \quad (11)$$

$$\sigma_{Px} \approx 0, \quad \sigma_{Py} \approx 0 \quad (12)$$

$$\theta_{S1} \approx \pi/2, \quad \delta\theta_{S1} = \theta_{S1} - \pi/2 \approx 0 \quad (13)$$

$$15 \quad \theta_{S2} \approx \pi/2, \quad \delta\theta_{S2} = \theta_{S2} - \pi/2 \approx 0 \quad (14)$$

$$\phi_{S12} \approx \pi/2, \quad \delta\phi_{S12} = \phi_{S12} - \pi/2 \approx 0 \quad (15)$$

Furthermore, we assume $\phi_a \approx 0$ without loss of generality. Dropping second order factors, we obtain the following linearized inverted matrices used in Equation (10):

$$\mathbf{G}^{-1} = \begin{pmatrix} 1/(gG_p) & 0 & 0 \\ 0 & g/G_p & 0 \\ 0 & 0 & 1/G_a \end{pmatrix} \quad (16)$$

$$20 \quad \mathbf{\Gamma}^{-1} = \begin{pmatrix} 1 & 0 & -\delta\theta_{S1} \\ -\delta\phi_{S12} & 1 & -\delta\theta_{S2} \\ 0 & 0 & 1 \end{pmatrix} \quad (17)$$

$$\mathbf{\Sigma}^{-1} = \begin{pmatrix} 1 & 0 & \sigma_{Px} \\ 0 & 1 & \sigma_{Py} \\ -\sigma_{Px} & -\sigma_{Py} & 1 \end{pmatrix} \quad (18)$$

$$\mathbf{\Phi}^{-1} = \begin{pmatrix} 1 & \phi_a & 0 \\ -\phi_a & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad (19)$$

Furthermore, without loss of generality, we assume the magnetic field in the despun (inertial) coordinate system (directions X , Y , and Z) to be in the X - Z -plane, and the spacecraft to spin around the Z -axis, which corresponds with the z -axis in the spacecraft fixed, spin aligned coordinate system (see Table 1). In that latter system, the field rotates and has the following form:

$$B_x = B_p \cos \omega t = B_X \cos \omega t \quad (20)$$

$$5 \quad B_y = B_p \sin \omega t = B_X \sin \omega t \quad (21)$$

$$B_z = B_a = B_Z \quad (22)$$

Here, ω is the angular frequency of the spacecraft rotation, usually determined from sun sensor or star tracker measurements, and t denotes the time. Inserting these relations in Equation (10) yields the expected temperature corrected output of the magnetometer in sensor coordinates. By applying the despun rotation matrix

$$10 \quad \mathbf{D} = \begin{pmatrix} \cos \omega t & -\sin \omega t & 0 \\ \sin \omega t & \cos \omega t & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad (23)$$

to Equation (10) to transform \mathbf{B}_{ST} into a non-orthogonal, despun coordinate system (directions X' , Y' , and Z' , see Table 1), after sorting by frequency and phase of the terms, and further dropping second order factors, we obtain the following relations.

They are structurally similar to Equations (11a), (11b), and (11c) in Kepko et al. (1996), but different in detail:

$$\begin{aligned}
B_{X'} &= \frac{B_p(1+g^2)}{2gG_p} \\
&+ \cos\omega t \left[O_{S1} + \frac{B_a(\sigma_{Px} - \delta\theta_{S1})}{gG_p} \right] \\
&- \sin\omega t \left[O_{S2} + \frac{gB_a(\sigma_{Py} - \delta\theta_{S2})}{G_p} \right] \\
5 \quad &+ \cos 2\omega t \left[\frac{B_p(1-g^2)}{2gG_p} \right] \\
&+ \sin 2\omega t \frac{B_p}{2G_p} \left[g\phi_a - \frac{\phi_a}{g} + g\delta\phi_{S12} \right]
\end{aligned} \tag{24}$$

$$\begin{aligned}
B_{Y'} &= -\frac{B_p}{2G_p} \left[\frac{1+g^2}{g} \phi_a + g\delta\phi_{S12} \right] \\
&+ \cos\omega t \left[O_{S2} + \frac{gB_a(\sigma_{Py} - \delta\theta_{S2})}{G_p} \right] \\
&+ \sin\omega t \left[O_{S1} + \frac{B_a(\sigma_{Px} - \delta\theta_{S1})}{gG_p} \right] \\
10 \quad &- \cos 2\omega t \frac{B_p}{2G_p} \left[g\phi_a - \frac{\phi_a}{g} + g\delta\phi_{S12} \right] \\
&+ \sin 2\omega t \left[\frac{B_p(1-g^2)}{2gG_p} \right]
\end{aligned} \tag{25}$$

$$\begin{aligned}
B_{Z'} &= \frac{B_a}{G_a} + O_{S3} \\
&- \cos\omega t \frac{B_p\sigma_{Px}}{G_a} \\
&+ \sin\omega t \frac{B_p\sigma_{Py}}{G_a}
\end{aligned} \tag{26}$$

- 15 These equations show how the parameters affect the signal content at the spin tone harmonics in the despun measurements. The first terms in all three Equations (24), (25), and (26) are the primary measurements terms. In the spin plane, the ambient magnetic field only has a $B_X = B_p$ component. Consequently, the first term of $B_{X'}$ is approximately B_p , while the first term of $B_{Y'}$ is approximately 0 as $\phi_a \approx 0$ and $\delta\phi_{S12} \approx 0$. In the spin axis, we find $B_{Z'} \approx B_a$ with $G_a \approx 1$ and $O_{S3} \approx 0$. In addition, superposed first and second harmonic signals are expected as functions of the calibration parameters. The first harmonic signals
- 20 are described by the second and third terms in Equations (24), (25), and (26). In the spin plane, Equations (24) and (25), the spin tone signals are the result of spin plane offsets $O_{S1/2}$ and projections of the spin axis field B_a onto the spin plane. In the spin axis, Equation (26), first harmonic disturbances are due to the projection of spin plane fields onto the spin axis, the reason being an incorrect description of the spin axis direction by the angles $\sigma_{P.x/y}$. Second harmonic signals are only expected in the despun spin plane components (fourth and fifth terms of Equations 24 and 25). These are due to a mismatch in spin plane gains
- 25 (parameter g) or an unaccounted non-orthogonality between the spin plane sensor axes S1 and S2 (parameter $\delta\phi_{S12}$).

Table 2. Parameters and favorable conditions

Group	Parameters	Disturbances	Conditions	Uncertainties
1	σ_{Px} and σ_{Py}	at ω along spin axis	high B_p , low F_a	$\Delta\sigma_{Px/y} \approx F_a/B_p$
2	g and $\delta\phi_{S12}$	at 2ω in spin plane	high B_p , low F_{2p}	$\Delta g \approx F_{2p}/B_p$ and $\Delta\phi_{S12} \approx 2F_{2p}/B_p$
3	O_{S1} and O_{S2}	at ω in spin plane	low B_a , low F_p	$\Delta O_{S1/2} \approx F_p + B_a\Delta\sigma_{Px/y} + B_a\Delta\theta_{S1/2}$
4	$\delta\theta_{S1}$ and $\delta\theta_{S2}$	at ω in spin plane	high B_a , low F_p	$\Delta\theta_{S1/2} \approx F_p/B_a + \Delta O_{S1/2}/B_a + \Delta\sigma_{Px/y}$

4 Favorable Conditions for the Determination of the Calibration Parameters

From the factors pertaining to the first and second harmonic terms of $B_{X'}$, $B_{Y'}$, and $B_{Z'}$ (Equations 24 to 26) it is possible to derive the conditions that should be favorable for the determination of the 8 previously mentioned parameters. These factors are:

$$5 \quad \left[O_{S1} + \frac{B_a(\sigma_{Px} - \delta\theta_{S1})}{gG_p} \right] \quad \text{and} \quad \left[O_{S2} + \frac{gB_a(\sigma_{Py} - \delta\theta_{S2})}{G_p} \right] \quad (27)$$

$$\left[\frac{B_p\sigma_{Px}}{G_a} \right] \quad \text{and} \quad \left[\frac{B_p\sigma_{Py}}{G_a} \right] \quad (28)$$

$$\left[\frac{B_p(1-g^2)}{2gG_p} \right] \quad \text{and} \quad \frac{B_p}{2G_p} \left[g\phi_a - \frac{\phi_a}{g} + g\delta\phi_{S12} \right] \quad (29)$$

Here, the factors (27) and (28) pertain to the spin tone disturbances in the despun spin plane and spin axis components, respectively, and (29) pertains to the second harmonic frequency disturbance (double spin tone frequency) in the spin plane components.

As can be seen, the first factor of the latter group (29) is dependent on B_p , the external field in the spin plane which we assume to be constant, on G_p , the absolute gain factor in the spin plane which should be approximately 1, and on $1/g - g$, which is 0 only if $g = 1$. Hence, the presence of one part of the second harmonic disturbance, though modulated by B_p , is ultimately dependent only on g , the ratio of spin plane gains. Consequently, this relation can be used to determine g correctly. The signal to do that and, in particular, the signal to noise ratio (SNR) is larger if B_p is larger. We capture this relation in the second line of Table 2. As the second harmonic disturbance in the spin plane is to be minimized to get g , the natural fluctuations around that frequency (of amplitude F_{2p}) should also be low in the spin plane. The uncertainty in g is then expected to be on the order of F_{2p}/B_p .

The same is true for the complementary factor, on the right side of (29): Also this second harmonic disturbance is modulated by B_p . When g is accurately determined, then the ϕ_a influence vanishes, and the entire factor can only vanish by correctly choosing $\delta\phi_{S12}$. Hence, to determine this parameter accurately, also B_p should be large and the natural fluctuations at the second harmonic should be of low amplitude (low F_{2p}). The uncertainty $\Delta\phi_{S12}$ of $\delta\phi_{S12}$ and, ultimately, ϕ_{S12} is expected to be on the order of $2F_{2p}/B_p$ (see line 2 in Table 2).

Let's focus on the group of factors (28). The spin frequency disturbance is clearly modulated by B_p , as G_a should be close to 1, so B_p benefits the SNR. These disturbances vanish if σ_{Px} and σ_{Py} become 0, i.e., if they are precisely determined. A low

amplitude in the natural fluctuations at the spin frequency along the spin axis F_a would also support the determination. The uncertainty in σ_{P_x} and σ_{P_y} is then expected to be on the order of $\Delta\sigma_{P_x/y} \approx F_a/B_p$ (line 1 in Table 2).

The first set of factors in (27) pertain to the spin frequency disturbances in the spin plane components. They consist of two parts: a spin plane offset component O_{S1} or O_{S2} , and a term that is modulated by B_a and which may vanish if the difference
5 $(\sigma_{P_x} - \delta\theta_{S1})$ or $(\sigma_{P_y} - \delta\theta_{S2})$ vanishes. Obviously, if B_a vanishes, then the spin plane spin frequency disturbances can only come from the spin plane offset components. Hence, for their determination it is beneficial if the spin axis field B_a is low and if the natural fluctuation level around the spin frequency in the spin plane F_p is low. The uncertainty in O_{S1} and O_{S2} is then expected to be on the order of $F_p + B_a\Delta\sigma_{P_x/y} + B_a\Delta\theta_{S1/2}$ (see line 3 of Table 2).

The remaining elevation angles $\delta\theta_{S1}$ and $\delta\theta_{S2}$ are most difficult to determine: it is beneficial if the spin axis field B_a is
10 high. In addition, however, it is necessary that the spin axis itself is well determined, as the parameters σ_{P_x} and σ_{P_y} equally influence the spin tone signal in the spin plane as $\delta\theta_{S1}$ and $\delta\theta_{S2}$. Note that σ_{P_x} and σ_{P_y} can be independently determined by minimizing the spin frequency disturbances in the spin axis component. F_p should again be low. Altogether, the uncertainty in $\delta\theta_{S1/2}$ is on the order of $\Delta\theta_{S1/2} \approx F_p/B_a + \Delta O_{S1/2}/B_a + \Delta\sigma_{P_x/y}$ (see line 4 of Table 2).

5 Parameter Determination

15 Based on the findings from the previous section, we propose algorithms to determine the 8 spin-related parameters in an iterative manner (sections 5.2 to 5.5). The algorithms are based on computing estimates of the parameters for short intervals, and evaluate the uncertainties of those estimates based on the uncertainties indicated in Table 2. Then, the estimates with uncertainties below a certain acceptable threshold are chosen to form the basis of one parameter correction.

5.1 Precalibration

20 The temperature dependent gains $\mathbf{G}_T(T_s, T_e)$ determined on ground should be used to convert the raw magnetometer output \mathbf{B}_S to a precalibrated, temperature corrected intermediate product \mathbf{B}_{ST} , according to Equation (8).

The offset vector \mathbf{O}_S and the calibration matrices Φ , Σ , Γ , and \mathbf{G} should be initiated with the best known values at the time of calibration. At the beginning, these will be ground obtained values:

- for θ_{S1} , θ_{S2} , ϕ_{S12} , and \mathbf{O}_S from ground magnetometer calibration,
- 25 – for ϕ_a from nominal spacecraft design or mirror/laser based alignment measurements,
- for σ_{P_x} and σ_{P_y} from an initial estimate of the spin axis direction (alternatively $\sigma_{P_x} = \sigma_{P_y} = 0$ may be chosen),
- and $G_p = G_a = g = 1$ due to precalibration.

If in-flight calibration has already taken place, then these values will be superseded by better in-flight determined values.

5.2 Calibration of the Spin Axis Direction

The entire interval of magnetic field measurements should be divided into small (overlapping) subintervals of length $t_{\text{int}} = 2\pi n/\omega$, with $n \in \mathbb{N}$. The factor n should not be too small; hence, the subintervals should contain a number of spin periods, so that the spin tone at the spin frequency and also the power around that frequency can be accurately determined. On the other hand, subintervals should not be too large, so that the field/environmental conditions can be assumed constant.

For each of the subintervals, the uncertainties $\Delta\sigma_{\text{P}x/y} \approx F_a/B_p$ need to be calculated (line 1 in Table 2). Conservatively, we choose B_p to be the minimal modulus of the spin plane field over the subinterval: $\min(\sqrt{B_x^2 + B_y^2})$. F_a can be estimated by taking the maximum of the discrete Fourier components $F_{a\pm}$ of the spin axis magnetic field B_z at frequencies ω_{\pm} that are slightly over and under the spin frequency: $\omega_{\pm} = 2\pi n_{\pm}/t_{\text{int}}$ with $n_{\pm} \in \mathbb{N}$ and slightly over/under n :

$$F_{a\pm} = \mathcal{F}(B_z, \omega_{\pm}) = \left| \frac{2}{N} \sum_{k=0}^{N-1} B_z(t_0 + k\delta t) \exp(-i\omega_{\pm} k\delta t) \right| \quad (30)$$

$$F_a = \max(F_{a\pm}) \quad (31)$$

Here t_0 is the start of a subinterval considered, N is the number of magnetic field measurement samples in that subinterval, and δt is the sampling period. The frequencies ω_+ and ω_- should sufficiently differ from ω to avoid leakage from spin tone. However, ω_+ and ω_- should also be close enough to ω so that the amplitudes at those frequencies resemble the natural amplitude level at the spin frequency. Note that the optimal choice of ω_+ and ω_- is subinterval specific. In practice, however, fixed frequencies can be used that are at some distance $|\omega_{\pm} - \omega|$, if that distance is safely larger than usual spin tone spectral peak widths.

From here on, we use $\mathcal{F}(B, \omega)$ to denote the Fourier component of B at frequency ω . It should be noted that it may be recommended to de-trend the B data before computing $\mathcal{F}(B, \omega)$, by simply subtracting a linear fit. Linear trends will not occur if the external field can be assumed to be constant. In many real applications, however, the spacecraft will move through field gradients during subintervals considered, and in these cases, the linear trend in the field measurements will increase the spectral content across the spectrum.

Parameter estimates $\sigma_{\text{P}x}$ and $\sigma_{\text{P}y}$ are determined by minimization of the spin tone S_a in the spin axis component: $S_a = \mathcal{F}(B_z, \omega)$. This minimization is performed for each subinterval. Hence, we obtain for each subinterval one estimate for $\sigma_{\text{P}x}$, for $\sigma_{\text{P}y}$, and for the uncertainty $\Delta\sigma_{\text{P}x/y}$. A final parameter update for $\sigma_{\text{P}x}$ and $\sigma_{\text{P}y}$ for the entire interval of interest may be obtained by selecting the most accurate subinterval estimates of those parameters, pertaining to minimal uncertainties $\Delta\sigma_{\text{P}x/y}$. From those estimates, the median or average may be computed. The selection of the best estimates can be threshold based with respect to $\Delta\sigma_{\text{P}x/y}$.

5.3 Calibration of Gain Ratio and Azimuthal Angle

As detailed in the previous section 5.2, an interval of interest is divided into short (overlapping) subintervals of length $t_{\text{int}} = 2\pi n/\omega$. For each of these subintervals, the uncertainties Δg and $\Delta\phi_{\text{S}12}$ are computed (see line 2 in Table 2). Therefore, the fluctuation amplitudes $F_{2p} = \max(\mathcal{F}(\sqrt{B_x^2 + B_y^2}, 2\omega_{\pm}))$ need to be computed, with $2\omega_{\pm} = 4\pi n_{\pm}/t_{\text{int}}$ and $n_{\pm} \in \mathbb{N}$

slightly over/under n . Subsequently, the parameters g and $\delta\phi_{S12}$ are determined for each subinterval by minimization of $S_{2p} = \mathcal{F}(\sqrt{B_x^2 + B_y^2}, 2\omega)$. From the set of g and $\delta\phi_{S12}$ estimates from all subintervals, those associated to lowest uncertainties can be chosen to yield final updates for g and $\delta\phi_{S12}$.

It should be noted that we are using here the modulus of the spin plane field ($\sqrt{B_x^2 + B_y^2} = \sqrt{B_{X'}^2 + B_{Y'}^2}$) to compute F_{2p} and S_{2p} instead of any individual spin plane component (B_X or B_Y) in a despun coordinate system, as would be suggested by the analytical treatment outlined in section 3. Both approaches (using the modulus or a despun component) are, however, mathematically equivalent. To show this, we can compute $\sqrt{B_{X'}^2 + B_{Y'}^2}$, using Equations (24) and (25). From the sum $B_{X'}^2 + B_{Y'}^2$, only those terms are large which contain the first term of Equation (24), because all other terms are products of multiple small factors and, hence, can be omitted due to linearization. Taking that into account, we obtain $\sqrt{B_{X'}^2 + B_{Y'}^2} \approx B_{X'}$. Hence, $\sqrt{B_x^2 + B_y^2}$ contains field and variations corresponding to the despun component, along which the external field is pointing. Evaluating $\sqrt{B_x^2 + B_y^2}$ is hence equivalent to evaluating B_X if the field points in the X -direction. This result is based on the assumption of the spin tone and second harmonic terms being small in comparison to the constant spin plane magnetic field, which should be fulfilled even in low field conditions if the initial set of calibration parameters is not too inaccurate. Note also that it is not possible to obtain additional information with respect to the calibration parameters by evaluating the field-perpendicular component B_Y , because the coefficients pertaining to the sin and cos terms of $B_{X'}$ and $B_{Y'}$ are the same (compare Equations 24 and 25).

The equivalence of the approaches (using the modulus or a despun component) brings up two questions: (i) Why did we not use the modulus when calculating the influences of the spin-related parameters in section 3 and (ii) why would we prefer using the modulus over a despun component here and in any practical application of the calibration algorithms outlined in this section 5? The answer to question (i) is that the mathematical treatment of the modulus is slightly more involved than the treatment of the individual despun coordinates. Furthermore, section 3 follows the approach of Kepko et al. (1996) who also use despun coordinates. Thereby, our results from section 3 become directly comparable to the results of their study. In their and our analytical treatments, the despinning process is exactly defined, perfectly known, and accurate. Hence, it does not introduce additional uncertainty into the calibration process. This latter statement is not true in any real application, which leads us to the answer of question (ii): The modulus of the spin plane field is readily available in any spinning coordinate system. Despinning is not necessary for magnetometer calibration, and it is not advised because it could introduce additional, unnecessary uncertainty.

5.4 Calibration of Spin Plane Offsets

The uncertainties for each subinterval are computed as suggested in line 3 of Table 2. Thereto, the maximum of the spin axis field ($B_a = \max|B_z|$) over each subinterval should be used. F_p is evaluated following Equation (31). Furthermore, estimates for the uncertainties $\Delta\sigma_{P_{x/y}}$ and $\Delta\theta_{S1/2}$ need to be obtained. These may be based on the variability of the selected estimates of $\sigma_{P_{x/y}}$ (see section 5.2) and $\delta\theta_{S1/2}$ (see next section 5.5) used to compute the final values of those parameters.

The offset estimates O_{S1} and O_{S2} are determined for each subinterval by minimization of $S_p = \mathcal{F}(\sqrt{B_x^2 + B_y^2}, \omega)$. From the set of O_{S1} and O_{S2} estimates, the most accurate can be chosen to compute final updates for the spin plane offsets. It should be

noted that the offsets are known to be the most variable parameters. Hence, it could be desirable to compute final offset updates more often than updates of other spin-related parameters, if possible.

5.5 Calibration of Elevation Angles

The uncertainties for each subinterval are computed as suggested in line 4 of Table 2, this time using $B_a = \min|B_z|$. Estimates for the uncertainties $\Delta\sigma_{P_{x/y}}$ and $\Delta O_{S1/2}$ need to be obtained, e.g., from the variability of selected $\sigma_{P_{x/y}}$ and $O_{S1/2}$ estimates. Subsequently, the elevation angles $\delta\theta_{S1}$ and $\delta\theta_{S2}$ are determined for each subinterval by minimization of $S_p = \mathcal{F}(\sqrt{B_x^2 + B_y^2}, \omega)$. From the set of $\delta\theta_{S1}$ and $\delta\theta_{S2}$ estimates, the most accurate can be chosen (lowest uncertainties) to yield final updates of those parameters.

It should be noted that the same quantity S_p is minimized to obtain the elevation angles $\delta\theta_{S1}$ and $\delta\theta_{S2}$ and the offset components O_{S1} and O_{S2} . Hence, the final selection of estimates according to the uncertainties $\Delta\theta_{S1/2}$ and $\Delta O_{S1/2}$, which are heavily dependent on $|B_z|$, is very important here. In low $|B_z|$, minimization of S_p yields the offset components, whereas in high fields the offsets do not matter any more and any spin tone may safely be attributed to an incorrect choice of the elevation angles, if the spin axis direction is precisely known.

5.6 Exclusion of Data Intervals

Certain intervals may be excluded from parameter determination, as some of the underlying assumptions may not be met well. For instance, intervals featuring large spacecraft/sensor temperature changes should be avoided, as parameters may vary within such intervals. Hence, uncertainties in the parameters may be significantly higher than what is reflected in the uncertainty estimates stated in Table 2. Large temperature variations are expected during eclipse intervals, where the spacecraft is in shadow (e.g., of Earth), and hours after eclipse intervals as temperatures relax to stationary values. Furthermore, magnetic field measurements at saturation levels need to be avoided. Lastly, intervals during and after spacecraft maneuvers may be problematic for calibration, as the spin axis will fluctuate during maneuvers and nutation may be visible for periods of time after maneuvers. It should be noted that all these considerations are spacecraft and orbit specific.

6 Application to THEMIS Data

To ascertain the accuracies that parameters may be determined with in different regions of near Earth space, on a highly elliptical orbit around Earth, we apply the algorithms detailed above to two days (20 and 21 July 2007) of THEMIS-C (Angelopoulos, 2008) fluxgate magnetometer (FGM) data (Auster et al., 2008). The data are available at 4 Hz sampling frequency (data product: FGL); they are already fully calibrated and the applied calibration parameters do not change over the two days considered. The magnitudes of the magnetic field along the spin axis $|B_z|$ and in the spin plane $\sqrt{B_x^2 + B_y^2}$ are displayed in Figure 2a in red and blue, respectively.

The different regions that THEMIS-C went through during these two particular days are best identified using the omnidirectional ion spectral energy flux densities, measured by the electrostatic analyzer (ESA, McFadden et al., 2008) and dis-

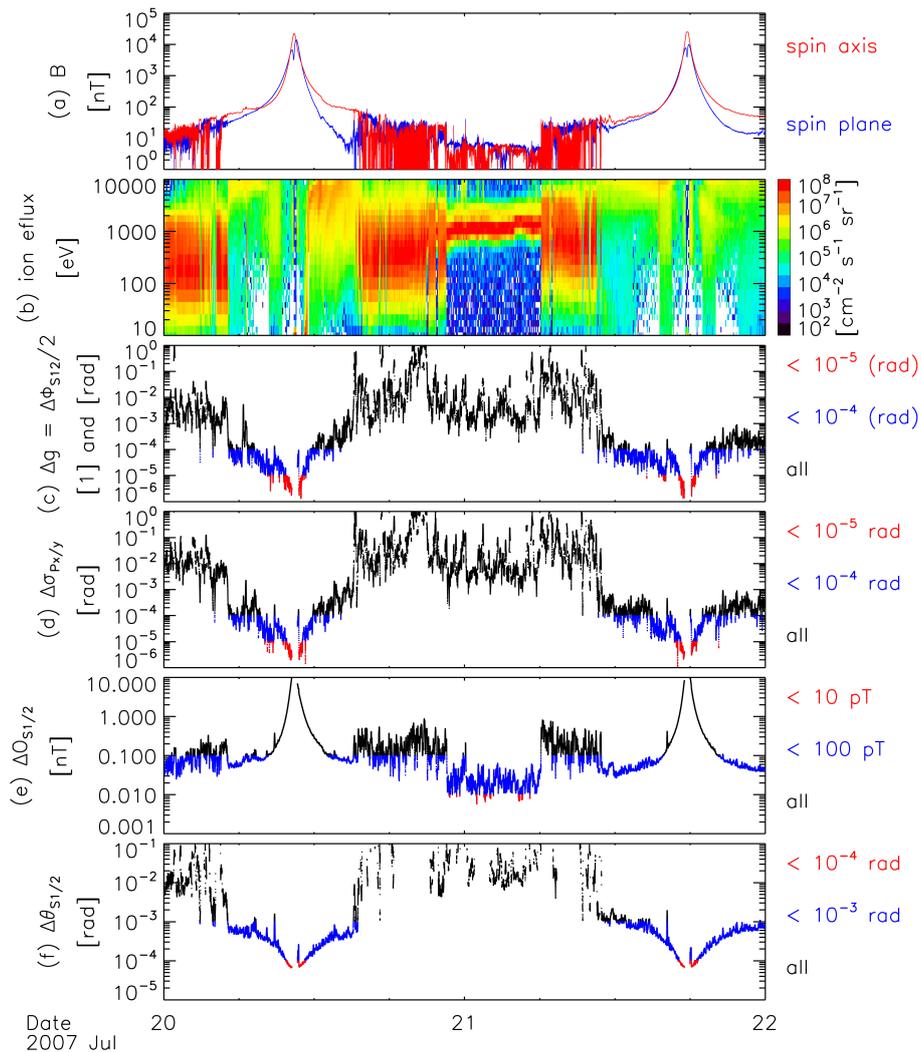


Figure 2. From top to bottom: (a) magnitude of the spin axis and spin plane magnetic fields in red and blue, (b) omni-directional ion spectral energy flux densities, (c) – (f) uncertainties of the estimates of the respective calibration parameters calculated in accordance to Table 2.

played in Figure 2b. At the beginning of 20 July 2007, THEMIS-C is located in the dayside magnetosheath. This is clearly visible in the broad ion energy spectrum which is characteristic for the thermalized solar wind plasma population present downstream of the bow shock. THEMIS-C fully transitions through the magnetopause into the magnetosphere at about 05:06 UT, moving inbound towards perigee at about 10:27 UT. At about 15:33 UT, THEMIS-C went back into the magnetosheath until about 22:33 UT, when it transitioned through the bow shock into the solar wind, characterized by a narrow energy signature corresponding to a cold plasma moving at the solar wind speed. On 21 July, THEMIS-C went back into the magnetosheath at about 06:07 UT, and then went further into the magnetosphere at about 10:53 UT. The perigee pass at that day took place at about 17:47 UT.

As can be seen in panel (a), the solar wind interval is characterized by low magnetic fields, typically below 10 nT. In the dayside magnetosheath, the field strength is somewhat higher, on the order of a few tens of nT, and highly fluctuating. Inside the magnetosphere, the fluctuation level is again low. The lowest field strengths of a few tens of nT are measured on the earthward side of the magnetopause, so just inside the inner magnetosphere. The field strength continuously increases towards Earth. On this particular THEMIS-C orbit, field strengths on the order of 10^4 nT are reached along the spin axis and in the spin plane close to perigee. As discussed above, both the fluctuation levels and field strengths have a major influence on the expected uncertainties of the calibration parameter estimates. We determine the parameters and the corresponding uncertainties for overlapping subintervals of 100 spin periods each, a spin period lasting for approximately 3 s. Hence, the subintervals have interval lengths of approximately 5 minutes. Note that we do not consider subintervals containing fields above $2 \cdot 10^4$ nT, due to FGM instrument saturation, and also excluded intervals in eclipse (Earth shadow) around perigee that lasted for approximately 22 min per orbit. Over the remaining times, temperature variations at the FGM sensor and electronics are limited to within 3 degrees. In the THEMIS case, these small variations are not expected to have a significant influence on the calibration parameters.

Subinterval lengths of 100 spin periods ensure good estimates of the power at around (and double) the spin frequency $\omega = 2\pi/(3\text{s}) \approx 2\text{rad/s}$, while the calibration parameters to be determined and the ambient magnetic field conditions may well be considered constant over such short intervals. Estimates of the power $F_{a\pm}$, $F_{p\pm}$, and $F_{2p\pm}$ around (double) the spin frequency are taken at 85% and 115% of ω and at 185% and 215% of ω , respectively. Following the equations from Table 2 and from the subsections 5.2 to 5.5 above, we determine the uncertainties for the calibration parameter estimates for all subintervals. They are shown in Figures 2c to 2f.

Figures 2c and 2d show the uncertainties $\Delta g = \Delta\phi_{S12}/2$ and $\Delta\sigma_{P_{x/y}}$. For the corresponding parameters, uncertainties on the order of 10^{-4} (rad) are generally acceptable. In the case of the gain ratio parameter g , an error of 10^{-4} would translate into an absolute error of 1 nT in 10000 nT fields. With respect to the angle ϕ_{S12} (or $\delta\phi_{S12}$) and to the spin axis angles $\sigma_{P_{x/y}}$, an error of $1 \cdot 10^{-4}$ rad is equivalent to approximately 0.5% of a degree. Uncertainties below 10^{-4} (rad) are marked in blue in Figures 2c and 2d. As can be seen, estimates of g , ϕ_{S12} , and $\sigma_{P_{x/y}}$ with uncertainties below this threshold can be obtained almost everywhere in the inner magnetosphere, where fields are relatively stable, but not in the magnetosheath (fluctuations too high) or in the solar wind (fields too low). Estimates associated with uncertainties below 10^{-5} (rad) are marked in red in Figures 2c and 2d. These are obtained only in the regions of highest ambient fields, close to perigee.

The parameter estimates themselves (g , $\delta\phi_{S12}$, σ_{P_x} , and σ_{P_y}) are shown in Figures 3a to 3d as a function of their respective uncertainties. Again, uncertainty thresholds of 10^{-4} (rad) and 10^{-5} (rad) are marked in blue and red, respectively. Taking the averages of the estimates associated with uncertainties below 10^{-5} (rad), we obtain:

$$\langle g \rangle = 0.99998 \pm 0.00004 \quad (32)$$

$$\langle \delta\phi_{S12} \rangle = (-3 \pm 6) \cdot 10^{-5} \text{ rad} \quad (33)$$

$$\langle \sigma_{P_x} \rangle = (-7 \pm 6) \cdot 10^{-5} \text{ rad} \quad (34)$$

$$\langle \sigma_{P_y} \rangle = (-1.7 \pm 0.4) \cdot 10^{-4} \text{ rad} \quad (35)$$

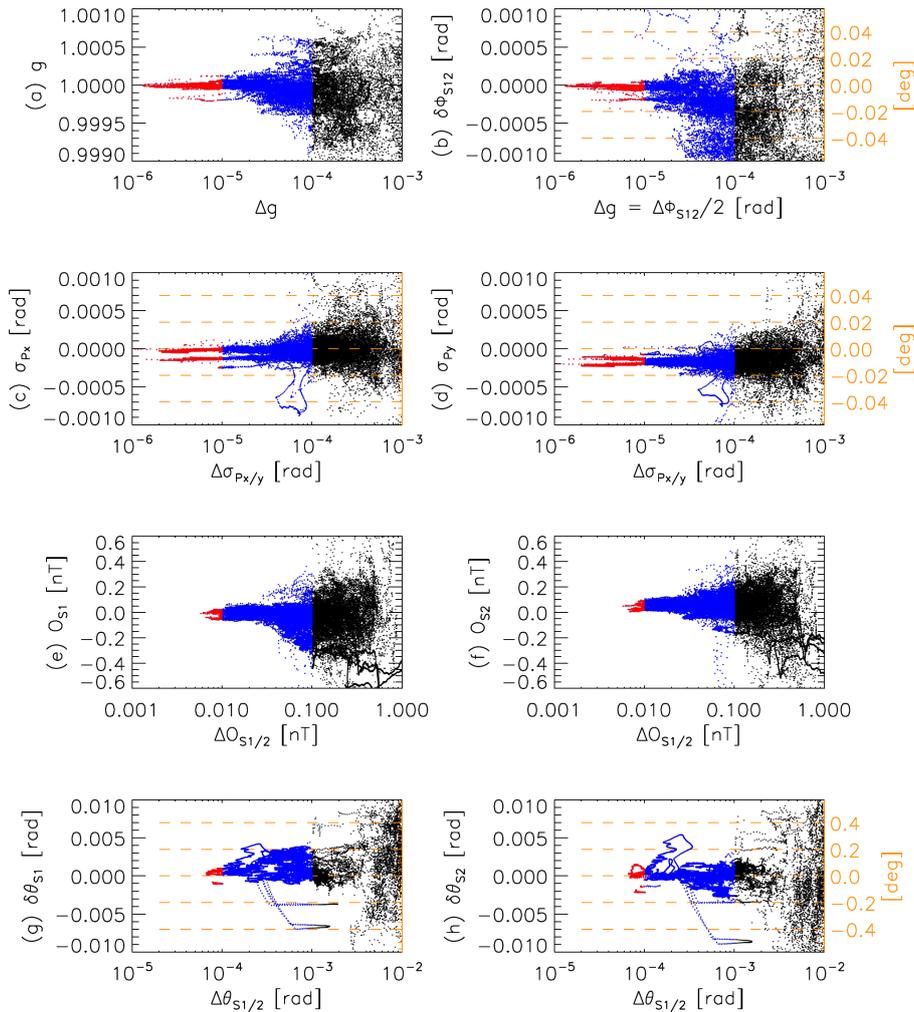


Figure 3. Calibration parameter estimates as a function of their respective uncertainties. Threshold levels for blue and red marked estimates are the same as in Figure 2. Panels (b) to (d), (g), and (h) have secondary axes in orange, showing parameter values in degrees.

Here, the error values are the corresponding standard deviations of the estimates. We see that all parameters are close to 0 (or 1 in the case of g); an update may only be advised for σ_{P_y} , as its deviation from 0 is significantly larger than the error value (see Figure 3d).

In Figures 3c and 3d, a split in values associated to low uncertainties can be clearly seen. A closer look on this phenomenon reveals that lower/higher $\sigma_{P_x}/\sigma_{P_y}$ values correspond to times before/after perigee passes. Hence, the spin axis direction in the orthogonalized sensor package coordinate system changes during perigee. This might be related to a temperature driven change in spacecraft geometry, i.e., in boom alignment to the spacecraft body, occurring in eclipse during perigee passes.

In order to calculate the uncertainties of the offset and elevation angle estimates ($\Delta O_{S1/2}$ and $\Delta\theta_{S1/2}$, see lines 3 and 4 in Table 2), we have to assume uncertainties in the knowledge of the spin axis direction angles ($\Delta\sigma_{P_{x/y}}$), the offsets ($\Delta O_{S1/2}$), and the elevation angles ($\Delta\theta_{S1/2}$). Based on Equation (35), we set $\Delta\sigma_{P_{x/y}} = 6 \cdot 10^{-5}$ rad. Furthermore, as we can justify a posteriori based on Equations (37) and (39), we set $\Delta O_{S1/2} = 25$ pT and $\Delta\theta_{S1/2} = 7 \cdot 10^{-4}$ rad. Therewith, we obtain the

5 uncertainty estimates per subinterval shown in Figures 2e and 2f.

The offsets directly influence the absolute accuracies of the magnetic field measurements. Typically, uncertainties on the order or below 0.1 nT are desired in low fields. Uncertainties meeting this threshold are marked in blue in Figure 2e. As can be seen, corresponding offset estimates can be routinely obtained in the solar wind, due to the low fields, and also in the outer, low field parts of the inner magnetosphere. Within the magnetosheath, however, many estimate uncertainties surpass the threshold

10 as the fluctuations levels are too high for accurate offset determinations. Estimates with uncertainties below 10 pT (in red) can only be obtained in the solar wind at low fields. From those (red dots in Figures 3e and 3f), we obtain average offsets of:

$$\langle O_{S1} \rangle = (-0.007 \pm 0.023) \text{ nT} \quad (36)$$

$$\langle O_{S2} \rangle = (0.036 \pm 0.025) \text{ nT} \quad (37)$$

The error values here motivate the choice of $\Delta O_{S1/2}$ for the computation of the uncertainties of the elevation angles. These

15 angles should also be known to the order of 10^{-4} rad. Unfortunately, estimates with uncertainties lower than this threshold are only obtained in very high fields, close to perigee, as can be seen by the red dots in Figures 2f, 3g, and 3h. The blue dots correspond to the lower threshold of 10^{-3} rad in this case, already equivalent to 5.7% of a degree in angular uncertainty. From the $\delta\theta_{S1/2}$ estimates pertaining to uncertainties lower than 10^{-4} rad we obtain the following averages:

$$\langle \delta\theta_{S1} \rangle = (5 \pm 4) \cdot 10^{-4} \text{ rad} \quad (38)$$

$$20 \quad \langle \delta\theta_{S2} \rangle = (3 \pm 7) \cdot 10^{-4} \text{ rad} \quad (39)$$

Within the group of sensor orthogonalization angles ($\delta\theta_{S1}$, $\delta\theta_{S2}$, and $\delta\phi_{S12}$) and spin axis angles (σ_{P_x} and σ_{P_y}), these elevation angles are least accurately defined. Apparently, it is difficult to determine them to accuracies on the order of 10^{-4} rad or better. When determined on ground, in higher fields, the parameters $\delta\theta_{S1/2}$ may however be better determined, with lower uncertainties than 10^{-4} rad. Hence, regular in-flight updating of these parameters may not be recommended, as those updates

25 may introduce unnecessary jitter without any benefit to the overall accuracy of the magnetometer calibration.

7 Discussion on Linearization Assumptions

The only purpose of linearizing the calibration equation in section 3 is to obtain the uncertainty relations shown in the right column of Table 2. These uncertainties ($\Delta\sigma_{P_{x/y}}$, Δg , $\Delta\phi_{S12}$, $\Delta O_{S1/2}$, and $\Delta\theta_{S1/2}$) are used to evaluate which calibration parameter estimates (from which subintervals) are most suitable to compute final calibration parameter updates. The estimates themselves are calculated using the non-linearized calibration Equation (9). Hence, simplifications and assumptions associated to linearization do not influence the accuracy of those estimates. They only influence the accuracy of their uncertainties!

To obtain these uncertainties, a series of assumptions need to be made, e.g., in the form of the relations (11) to (15). This approach raises the question of how much the calibration parameters may be allowed to deviate from the assumed values. As shown in the previous section 6, we are interested in the orders of magnitude (factor of 10) of the uncertainties $\Delta\sigma_{P_x/y}$, Δg , $\Delta\phi_{S12}$, $\Delta O_{S1/2}$, and $\Delta\theta_{S1/2}$. Conservatively limiting the errors in these uncertainties to a factor of 2, and taking into account the multiplication of parameters due to Equation (10), we can allocate lower limit individual admissible error factors of $\sqrt[4]{2} = 1.189$ to gain factors g , G_p , and G_a , as well as angles σ_{P_x} , σ_{P_y} , $\delta\theta_{S1}$, $\delta\theta_{S2}$, $\delta\phi_{S12}$, and ϕ_a . Such error factors of 1.189 or, equivalently, deviations by 19% from the assumed values are extraordinarily large when compared to the accuracy in the knowledge of the calibration parameters and of the geometry of the sensor and spacecraft, even before performing any in-flight calibration. For the angles, this means that deviations from 0 by up to 11° are acceptable ($\arcsin(19\%)$); note that alignment uncertainties and deviations from sensor orthogonality should usually be lower than 1° . For the gains, deviations by 19% would be acceptable; ground calibration, however, should reduce these deviations to less than 0.1%. Hence, the assumptions made to linearize the calibration equation are not restrictive at all and can easily be fulfilled in practice.

8 Further Discussion and Conclusions

The orthogonalization angles are known to be relatively stable when compared to the spin axis direction angles. Fortunately, as shown in section 6, the spin axis angles can be updated with high accuracy more regularly than the sensor elevation angles $\delta\theta_{S1}$ and $\delta\theta_{S2}$. The parameter decoupling introduced in section 2 pays off here, as spin axis variations do not require re-determination of the sensor elevation angles as would be the case when using the calibration Equation (1) with the coupling matrix (2) instead of Equation (9).

It should be noted that both Equations (1) and (9) assume raw magnetometer outputs to be linearly transformable into accurate magnetic field estimates. This assumption of linearity can only be fulfilled to a certain degree when dealing with actual magnetometer hardware. Non-linearities (e.g., Auster et al., 2008; Russell et al., 2016) will adversely affect the calibration as described here if not characterized, quantified, and corrected beforehand, as they produce spin tone and higher harmonic signals in the magnetic field measurements. THEMIS FGM data, for instance, suffer from slight non-linearities in digital-to-analogue converters that are part of the magnetometer hardware. These are known from ground characterization of the instruments and are routinely corrected in advance of any in-flight calibration activities and/or any conversion of magnetometer outputs into calibrated magnetic field measurements (Auster et al., 2008).

Assuming instrument linearity, the uncertainty-based approach to determining the spin-related calibration parameters allows for a meaningful estimation of the error alongside with any parameter updates. These errors can be compared to the uncertainties of the already known parameters, determined either on ground or in-flight. Therewith, it is possible to decide whether any update of the calibration parameters is necessary/advised or, instead, would just introduce unnecessary variations in the calibration parameters over time.

In addition, the availability of calibration parameter estimates associated to low uncertainties, sufficient in number and quality, determines what is possible in terms of cadence of parameter updates. This availability depends on the orbit of the

spacecraft (the presence in regions of certain field conditions), and also on the spin period of the spacecraft. In general, short spin periods (high spacecraft spin frequencies) are favorable, as they increase the number of spins that may be taken into account in subintervals of certain length. A larger number of spin periods reduces the influence of natural field fluctuations at (double) the spin frequency, while short subinterval lengths ensure the constancy of the parameters and environmental
5 conditions. In the given THEMIS-C example, the spin plane offsets $O_{S1/2}$ may be continuously tracked while the spacecraft remained in the solar wind and in the low field parts of the magnetosphere. The spin axis components $\sigma_{Px/y}$, the gain ratio g and azimuthal orthogonalization angle ϕ_{S12} can easily be determined separately before/after each perigee pass, whereas accurate determinations of the elevation angles $\theta_{S1/2}$ may only be possible when taking into account estimates from several spacecraft orbits.

10 Finally we would like to note that the benefits of parameter decoupling (i.e., a sensible choice of parameters when taking into account the behavior of the magnetometer and spacecraft hardware) and of the uncertainties-based determination of those parameters are not tied to the exact definitions of the calibration Equation (9) and matrices (4) to (7). For example, the offsets may be applied in an orthogonal, spacecraft-fixed coordinate system instead of in the sensor coordinate system, if the main contribution to the offsets is expected from spacecraft stray fields at the sensor position. The order of the gain, orthogonalization,
15 and alignment matrices (here \mathbf{G} , $\mathbf{\Gamma}$, $\mathbf{\Sigma}$, and $\mathbf{\Phi}$) may be changed, and/or the 12 degrees of freedom of the calibration parameters may be distributed over a larger number of matrices and offset vectors to account for changes pertaining to different parts of the magnetometer/spacecraft system in different coordinate systems (e.g., see equations in Fornaçon et al., 1999; Auster et al., 2008). Hence, while following the principles set out in this paper, a different set of calibration parameters and corresponding calibration equation may be specifically selected for each magnetometer/spacecraft combination.

20 *Data availability.* Data from the THEMIS mission including FGM and ESA data are publicly available from the University of California Berkeley and can be obtained from <http://themis.ssl.berkeley.edu/data/themis>.

Competing interests. The authors declare that they have no conflict of interest.

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