

Steering recoverable autonomous sonde (RECAS) for accessing and studying subglacial lakes

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Abstract

 The study of subglacial lakes requires clean access and sampling technologies. One of the most promising alternatives is the newly developed hot-point RECoverable Autonomous Sonde (RECAS), which allows downward and upward ice drilling and subglacial water sampling while the subglacial lake remains isolated from the surface. The original sonde descends downward under the force of gravity, and the borehole trajectory cannot be controlled. However, in certain cases, the sonde would preferably be able to drill at specific angles and directions, enabling it to follow a desired trajectory (e.g., maintaining verticality within the desired range) or bypass obstacles in the ice (e.g., stones and other inclusions). The general principle for the steering RECAS is to adjust the voltage for the electric thermal head heaters, which provides an opportunity to control the heat distribution on the drill head surface, thereby altering borehole trajectory during drilling. In this paper, the general principles of steering RECAS are described, and experimental results on deviational ice drilling with a controllable electric thermal head are discussed.

Keywords

- Ice drilling technology; Subglacial lakes; Clean access sampling; Thermal sonde;
- Steerable system

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1. Introduction

 It is now widely accepted that subglacial hydrological environments are similar to the water distribution found elsewhere on Earth's surface and comprise a vast network of lakes, rivers, and streams located thousands of metres beneath ice caps, glaciers, and the Antarctic and Greenland ice sheets (Bowling et al., 2019; Siegert et al., 2012). A subglacial lake is considered to be any large body of liquid water existing below an ice mass. The water depth of subglacial lakes varies from a few to several hundred metres. As of 2022, a total of 773 subglacial lakes have been identified, including 675 in Antarctica, 64 in Greenland, two beneath the Devon Ice Cap, six beneath Iceland's ice caps, and 26 in valley glaciers (Livingstone et al., 2022). The ice thickness above subglacial lakes may vary from several tens to thousands of metres.

 Subglacial lakes provide unique information regarding paleoclimatic conditions, basal hydrology, biogeochemical fluxes, and geomorphic activity. It is anticipated that subglacial lakes harbour relict microbial species capable of thriving in complete darkness, low nutrient levels, high water pressures, and isolation from the atmosphere (Skidmore, 2011). In-situ investigations should not contaminate these subglacial aquatic systems. Currently, hot-water drilling systems are considered the cleanest method for accessing subglacial lakes. US teams successfully accessed the Whillans and Mercer subglacial lakes on the coastal margin of West Antarctica in early 2013 and during the 2018-2019 season, demonstrating the well-proven effectiveness of this technology (Priscu et al., 2021; Tulaczyk et al., 2014).

 However, access technology using hot-water drilling systems has several significant drawbacks. For instance, these systems necessitate complicated methods to filter and subject high- speed hot-water flow (>150-200 L/min) to ultraviolet (UV) treatment at the surface. Additionally, they are extremely bulky and highly power-consuming. To simplify the drilling process and decontamination of drilling tools, we propose accessing and studying subglacial lakes with a freezing-in electric hot-point thermal drill — the RECoverable Autonomous Sonde (RECAS) — capable of downward and upward ice drilling and subglacial water sampling while ensuring that

 the subglacial lake remains isolated from the surface (Talalay et al., 2014). RECAS is estimated to be 10-20 times less expensive than penetration with a hot-water drilling system, and its installation and operation require only four specialist staff members (Sun et al., 2023). The sonde surface is thoroughly cleaned before deployment. Although the sonde might drag native microbes, which are embedded in ice, into subglacial targets at various depths as they melt, this occurs in a predictable manner (Schuler et al., 2018). Two concepts similar to RECAS have been proposed by Stone Aerospace, a US engineering company (Pereira et al., 2023; Stone et al., 2018), and Aachen University in Germany (Heinen et al., 2021).

 The RECAS was successfully tested in East Antarctica during the 2021-2022 field season, reaching the ice-sheet base at a depth of 200.3 m, sampling basal meltwater and measuring its pressure, temperature, pH, and conductivity before returning to the ice surface (Sun et al., 2023). To expand the sonde's possibilities, we propose equipping it with a steering technique to control and guide the drilling process. This allows drilling at specific angles, depths, and directions, enabling the sonde to follow a desired trajectory (e.g., maintaining verticality within the desired range) or bypass obstacles in the ice (e.g., stones and other inclusions). Herein, we describe the general principles of the steering RECAS and discuss the experimental results on deviational ice drilling with a controllable electric thermal head.

2. Steering approaches of the RECAS

2.1. General concept of the steering RECAS

 The RECAS comprises four major systems: a heating system (consisting of an upper melting head, a lower melting head, and lateral heaters), an inner winch system, a scientific load platform, and a parameter detection and control system (Sun et al., 2024). The upper and lower thermal heads are identical except for the central hole of the cable in the top thermal head (Li et al., 2020). Thus, it can drill both downward and upward and move within the borehole using an inner cable-recoiling mechanism, similar to how a spider climbs on its silk line.

- Two RECAS prototypes were developed: RECAS-200, with a 200-m-long cable inside, and RECAS-500, with a 500-m-long cable inside. The RECAS-500 design is shown in Fig. 1. The prototypes differed not only in their drilling ability but also in their sizes, power consumption, number of cartridges in the thermal drill head, etc. (Table 1). In both prototypes, all heaters are supplied simultaneously at the same voltage from a single source.
- **Table 1**
- General parameters of RECAS-200 and RECAS-500

 The fundamental principle behind an adjustable electric thermal head is to control the voltage supplied to each pair of adjacent heaters. This enables control over the heat distribution on the drill head surface and allows borehole deviations during drilling. Furthermore, controlling the heat distribution of the thermal head makes it possible to equalise the load on the heaters as needed. Heating cartridges exhibit variations in their parameters owing to their technological tolerances. Additionally, these parameters may change slightly during long-term use, and heating cartridges can fail because of their long-term use or manufacturing defects.

 The sonde is steered using data from an inclinometer installed inside it. The data from the inclinometer are transmitted to a personal computer (PC), processed, and converted into pulse- width modulation (PWM) coefficients, which determine the PWM duty cycle for a specified number of channels. In the subsequent tests using the RECAS-200 prototype, the PC will be replaced with a microcontroller mounted inside the sonde. The PMW coefficients are transmitted from the computer to a PWM generator (Sup. 2) inside the sonde prototype, where an individual PWM signal is generated for each channel. Each PWM signal is amplified using a power module (Sup. 3) and supplied to the corresponding heater inside the drill head. The PWM signal duty cycle limits the heater power.

99 101

100 **Fig. 1.** General schematic of the RECAS-500 with a 500-m-long cable inside (all dimensions are in mm)

102 *2.2. RECAS positioning estimation*

 The following method was employed to convert the values received from the inclinometer into PWM coefficients. The inclinometer transmitted deviation values along the *X* and *Y* axes. As shown in Fig. 2, the *X* and *Y* axes correspond to the inclinometer axes in the horizontal plane. Point *A* indicates a deviation, with *X* = 4.5 and *Y* = −3, for instance. Eight pairs of 16 heaters are shown schematically in the form of circles, designated as *H1*-*H8*.

108

109 **Fig. 2.** Schematic diagram of the heaters *H1*-*H8* relative location and inclinometer in the sonde prototype.

110 First, the absolute inclination φ is determined (Eq. 1). This value is required not only for

111 subsequent calculations but also for monitoring purposes.

$$
\varphi = \sqrt{X^2 + Y^2} \tag{1}
$$

112 where *X* and *Y* are the coordinates received from the inclinometer.

113 Next, the projection length values *lⁿ* of point *A* on the axis of each pair of heaters are

114 determined as follows (indicated in red in Fig. 2):

$$
l_n = \varphi \cos\left(\arctan\left(\frac{Y}{X}\right) - \alpha_n\right) \tag{2}
$$

115 where α_n is the heater axis angle relative to the *X* and *Y* axes.

- 116 To obtain the required PWM coefficients, the *lⁿ* values must be converted to relative values 117 in the range of 0-1. Additionally, it is necessary to be able to adjust the resulting coefficients. For 118 this purpose, a logistic function (logistic curve) was used (Kyurkchiev et al., 2015). After slight
- 119 adaptation to meet our conditions, the final equations take the following form:

$$
K_n = \frac{1}{1 + \exp(-T(l_n + V))}; \ V = \frac{1}{T} \ln \frac{-y_{\text{off}}}{y_{\text{off}} - 1}
$$
(3)

- 120 where K_n is the PWM coefficient for each heater pair, *V* is the intermediate coefficient, *T* is the 121 correction coefficient (above zero), and *yoff* is the offset coefficient (0-1).
- 122 *T* and y_{off} are used to adjust the final values. The coefficient y_{off} limits the maximum average 123 PWM coefficient value (i.e., with zero inclination and $y_{\text{off}} = 0.5$, all PWM coefficients will be 0.5). 124 Meanwhile, the correction coefficient *T* affects the rising section length where the derivative is 125 relatively large. The influence of *T* and *yoff* on the final results is illustrated by the example 126 discussed next.

127 *2.3. RECAS positioning calculation example*

128 For the calculation example, random inclinometer values are taken as: *X* = 4.5; *Y* = −3. Then,

129 absolute inclination is

130
$$
\varphi = \sqrt{X^2 + Y^2} = \sqrt{4.5^2 + (-3)^2} = \sqrt{20.25 + 9} = \sqrt{29.25} = 5.41.
$$

131 The α values for eight heater pairs are presented in Table 2.

132 **Table 2**

133 The α values for eight pairs of heaters

134 The projection length of the first heater is estimated as

135
$$
l_1 = \varphi \cos\left(\arctan\left(\frac{Y}{X}\right) - \alpha_1\right) = 5.41 \cdot \cos\left(\arctan\left(\frac{-3}{4.5}\right) - 0\right) = 5.41 \cdot \cos(-33.69) = 5.41 \cdot 0.83 = 4.5
$$
.

136 The calculation results for all eight projection length values are listed in Table 3 and shown

137 in graph form in Fig. 3.

151

152 **Fig. 4.** PWM coefficients at constant $X = 4.5$; $Y = -3$; $y_{\text{off}} = 0.5$, and three different values of $T = 0.5$; $T = 1$; $T = 2$.

3

 $T = 0.5$

 0.3 0.2 0.1

 \circ

 $T = 2$

 $\overline{2}$

8

153

154 **Fig. 5.** PWM coefficients at constant $X = 4.5$; $Y = -3$; $T = 1$, and three different values of $y_{off} = 0.2$; $y_{off} = 0.5$; $y_{off} = 0.8$. 155 The coefficients *T* and *yoff* should be selected experimentally. Therefore, they do not need to 156 remain constant. They may depend on other parameters; for example, *yoff* may depend on the 157 absolute inclination. It is worth noting that when the correction coefficient *T* approaches zero, all 158 PWM coefficients tend towards the *yoff* value, which means that the heat distribution on the drill 159 head surface approaches a uniform pattern.

160 **3. Passability of the RECAS**

 Before changing the borehole trajectory direction, determining the passability of the sonde in the drilled borehole is essential. Owing to its length exceeding 7 m, the RECAS has a high likelihood of becoming stuck in the borehole, even with relatively small deviations. The main parameter affecting sonde passability in a curved borehole is the deviation intensity. To characterise the borehole deviation intensity at a specific interval along its axis, the relative zenith angle values were used, considering the interval between their measurement points. Therefore, the zenith deviation intensity was determined as follows (Zvarygin, 2010; Shamshev et al., 1983):

$$
i_{\theta} = \frac{\Delta \theta}{\Delta L} \tag{4}
$$

168 where $\Delta\theta$ is the relative zenith angle in degrees and ΔL is the borehole axis interval length.

169 If the deviation intensity at some borehole interval remains constant $(i_{\theta} = const)$, it means 170 that the borehole is curved along a circular arc at a certain interval. The borehole radius of 171 curvature *R* depends on the deviation intensity, as follows (Fig. 6):

$$
R = \frac{57.3}{i_{\theta}}\tag{5}
$$

172

173 **Fig. 6.** Schematic of the stuck sonde in a curved borehole.

174 The passability of a sonde in a borehole interval with known diameter and radius of curvature

175 can be determined as follows:

$$
l_{s} \leq \sqrt{8R(D_{b}-D_{s})-4(D_{s}-D_{b})^{2}}
$$
\n(6)

176 where l_s is the length of the cylindrical part of the sonde (the thermal head length is not included),

177 D_s is the sonde diameter, and D_b is the borehole diameter.

178 As the borehole radius of curvature is considerably larger than the gap between the sonde 179 and borehole diameters, Eq. 6 can be simplified as follows (Shamshev et al., 1983):

$$
l_s \leq \sqrt{8R(D_b - D_s)}\tag{7}
$$

180 Based on RECAS field tests, the difference between the borehole and sonde diameters are 181 10-20 mm. This clearance mainly depends on the rate of penetration (ROP), and additional 182 laboratory tests are required to establish a more precise relationship. Considering that the RECAS

- 183 length is approximately 7 m, the range of radii of curvature ensuring RECAS passibility is in the
- 184 range of 300-600 m.
- 185 Therefore, it is not sufficient to simply monitor the borehole inclination to avoid the RECAS
- 186 from being stuck in the borehole. Instead, it is necessary to continuously estimate the deviation
- 187 intensity, the borehole radius of curvature, or both at an interval from the bottom hole with a length
- 188 approximately equal to that of the sonde.

189 **4. Testing stand and sonde prototype design**

- 190 *4.1. Testing stand*
- 191 *4.1.1. General testing stand design*

192 The testing stand consists of a sledge, mast, top wheel, winch, and sonde prototype (Fig. 7).

193 All stand parts are mounted on a sledge, which has a modular construction comprising a pair of

194 skis and two welded frames bolted together. A 2-m-high mast is mounted in the middle of the

195 sledge. A small winch is mounted near the mast on a sledge. A block is installed at the top of the

196 mast. The testing stand parameters are listed in Table 5.

197 **Table 5**

198 Testing stand parameters

Fig. 7. Schematic of the testing stand

4.1.2. Top block and as-low-as-practicable ROP

 The top block consists of two wheels – a measuring wheel and a guiding wheel, an encoder, and two load-cell sensors. The measuring wheel is designed for a rope with a 5 mm diameter so 205 that the cable length passing through the wheel per revolution equals $1 \text{ m } \pm 1 \text{ mm}$. This design simplifies the calculation and further adjustment of the measuring equipment. The guiding wheel is used to guide the rope from the winch to the measuring wheel.

 To register the weight on bit (WOB), two load-cell sensors are installed underneath the top wheel. Each sensor can withstand a force of up to 100 daN. To measure the ROP, an encoder with an accuracy of 5000 measurements per revolution (MPR) is installed on the measuring wheel shaft. As the ROP is expected to be relatively low, the angular rotation speed of the measuring wheel is

- 212 correspondingly small. Therefore, the higher the encoder accuracy, the more frequently it can
- 213 capture instantaneous low-ROP values.
- 214 As-low-as-practicable ROP [m/h] can be estimated as follows:

$$
\nu_{\min} = 3600 \cdot \pi \left(D + d \right) n_{\min} \tag{8}
$$

- 215 where *D* is the wheel diameter ($D = 0.3135$ m); *d* is the rope diameter, and n_{min} is the minimum angular
- 216 velocity in revolutions per second (RPS)
- 217 Minimal angular velocity n_{min} is equal to:

$$
n_{\min} = \frac{1}{tm} \tag{9}
$$

- 218 where *m* is the encoder accuracy in MPR and *t* is the time after which the data must be updated (in
- 219 this study, $t = 1$ s).
- 220 The wheel diameter is:

$$
D = \frac{l}{\pi} \tag{10}
$$

- 221 where *l* is the wheel circumference.
- 222 After all rearrangements, the as-low-as-practicable ROP is:

$$
\upsilon_{\min} = 3600 \cdot \frac{l}{tm} \tag{11}
$$

223 Therefore, the as-low-as-practicable ROP, which can be measured with a 5000-MPR encoder,

224 1-m wheel circumference, and a measurement frequency of once per second, was 0.72 m/h.

225 *4.1.3. Winch*

 The winch is based on an RV50 series worm gearbox. For precise winch control, a 200-W power servo drive was chosen in this study. To compensate for the low servo power, a small PX60 series planetary gearbox with a gear ratio of 1:6 was installed between the worm gearbox and servo. The small drum was customised to hold one layer of 5-mm-diameter Kevlar rope with a length of 10 m. To simplify the winch construction, the drum was mounted directly on the output shaft of the worm reducer. Further details regarding the winch construction design are presented in Sup. 1.

232 *4.1.4. Control system*

 The control system consists of a box containing various data acquisition modules (Fig. 8). Data acquisition modules ADAM 4017+ and ADAM 4018+ were used to collect data from the load-cell sensors and thermocouples, respectively. Counter-tachometer module CTA4001A was used to receive and convert signals from the encoder on the measuring wheel. Two MIK-1100 modules were connected to voltage and current sensors. Temperature module DT320 was used to monitor the sonde prototype drill head temperature. All modules, along with the voltage and current sensors, were mounted in a BDH20016 black case. The wiring schematics for all components are shown in Fig. S5.1 (Sup. 5). The sensor parameters are listed in Table 6.

241

243 **Table 6**

244 Parameters of the sensors

4.1.5. Software

 The control system box, servo control unit, and drill head control unit were connected to a computer via RS-485. The MODBUS RTU communication protocol was used for data transmission. The software registers the following parameters from the sensors connected to the control system box: ROP (m/h) and Depth (m) (Section 2 in Fig. 9); WOB (daN) (Section 3); Current (A), Voltage (V), Power (W), and three temperatures (°C) (Section 5). Through the drill head control unit, the software allows monitoring of the sonde prototype inclination and heater status and allows selection between manual and automatic modes (Section 4). A control panel for the winch is located at the bottom of the screen (Section 6).

4.2. Testing sonde prototype

4.2.1. General structure of the sonde prototype

 The sonde prototype consisted of a thermal drill head borrowed from the RECAS-200 prototype and a control unit assembled inside the housing (Fig. 10). The total sonde prototype

- length was approximately 1.1 m, and its weight was approximately 35 kg. The sonde prototype
- was suspended using a Kevlar rope tied to a hook. Electric lines for the power supply and
- communication were inserted through isolated connectors in the top cover.

Fig. 10. Schematic of the self-steering sonde prototype

4.2.2. Thermal drill head

 The thermal head diameter was 160 mm. It had 16 heat cartridges with a total power of approximately 7.6 kW (Li et al., 2020; Talalay et al., 2019). The heaters connections in the thermal drill head were redesigned (Fig. 11). Fuses were installed on each heater, and a distribution board was designed to distribute the load and connect it to the power connector (Fig. 12). To allow each heater to be individually connected to a power source, the power connector was also changed from two four-pin connectors to one 21-pin connector.

277

278 **Fig. 12.** Electrical schematic of thermal drill head

P

 \overline{D}

LD-POH-6.200 400V 540W

LD-POH-6.150 400V 410W

LD-POH-6.200 400V 540W

LD-POH-6.150 400V 410W

 The thermal drill head uses eight long heaters (200 mm in length) and eight short heaters (150 mm in length) that were arranged in an alternating pattern. The cartridges were controlled in pairs, with each long heater paired with an adjacent short one (Fig. 12). Therefore, the number of required PWM signals (PWM channels) was reduced to eight.

FUSE 4A 500V

FUSE 3A 500V

FUSE 4A 500V

FUSE 3A 500V

╕

 $CH1-CQ$

 C H7 - OP

 $_{\sim}$ COM

 $\overline{}$ COM

- *4.2.3. Control unit*
- To control the heaters in the sonde prototype, a control unit was designed as a pressure
- chamber housing the following components (Fig. 13).

 Dual axis inclinometer. A two-axis inclinometer was chosen instead of a three-axis one because the control unit was rigidly fixed together with the thermal drill head inside the sonde prototype, eliminating the need to track the relative rotation along the vertical axis. The task of tracking the borehole azimuth is planned for future RECAS prototype testing.

 PWM generator for 20 channels (Sup. 2). Although only eight PWM channels were required in this study, the PWM generator was designed with 20 channels to enable the control of individual heaters in the bottom drill head in the RECAS prototype in the future.

 Two power modules, 4 channels each (Sup. 3). The heater pairs were not connected directly to the PWM generator but through power modules that amplify the corresponding PWM signals from the generator.

 Two 15-volt DC-DC converters (Sup. 4). Two identical DC-DC converters were used to isolate the power supply of the inclinometer and the PWM generator from the power supply of the low-voltage part of the power modules.

The wiring schematics for all components are shown in Fig. S5.2 (Sup. 5).

- 302 All control unit modules, except for the inclinometer, were customised for this study. The
- 303 primary characteristics of the control units are listed in Table 7.

304 **Table 7**

305 Control unit main parameters

306 Further details regarding each individually designed module can be found in the

307 corresponding supplements.

308 **5. Laboratory testing of self-steering sonde prototype**

309 *5.1. Factors and main parameters of experiments*

310 To study the sonde prototype inclination in a drilled borehole, a series of tests were

- 311 conducted in the Polar Research Center laboratory.
- 312 The main factors affecting the sonde inclination and drilling performance are:
- 313 1. Ice temperature (kept constant at −16°C);
- 314 2. Environmental temperature (varied slightly between $+7^{\circ}$ C and $+12^{\circ}$ C);

315 3. ROP, which was controlled by the winch and limited by the power supplied to the heaters

- 316 inside the drill head;
- 317 4. WOB, which changed with the ROP and was limited by the sonde prototype weight.

318 The main parameter to be recorded was the sonde inclination. The sonde inclination was

- 319 affected by the controlled heat distribution on the drill head surface, which was controlled by
- 320 limiting the heater power. The control algorithm, with two variable coefficients *T* and *yoff* is
- 321 described in Eq. 3. Therefore, the main purpose of the experiments was to determine the
- 322 dependence of the sonde inclination on these coefficients. For clarity and visual control, blocks of
- 323 transparent ice with dimensions of $50 \times 50 \times 100$ cm were used in the experiments (Fig. 14).

Fig. 14. Testing of the sonde prototype with RECAS-200 controllable thermal head

5.2. Preliminary experiment

 A preliminary experiment was conducted to determine the potential ROP and WOB ranges and the possibility of controlling the sonde prototype inclination in the borehole by regulating the heater power in the drill head. The experiment recording was divided into four sections (Fig. 15).

Fig. 15. Recording of the preliminary experiment

 Section 1 (0-6 min). The first 200 mm of drilling were strictly vertical, with an ROP of 0.6 m/h and all heaters running at 50% power. Subsequently, the power was increased, and the ROP was increased to 1 m/h. Then, half of the heaters on one side of the thermal head were switched off.

 Section 2 (6-11 min). No sonde prototype inclination was detected, and the ROP was set to 2 m/h to increase the WOB.

 Section 3 (12-16 min). The inclination began to increase rapidly when the WOB value reached approximately 25 daN. An attempt was made to stabilise the WOB at this value. The WOB stabilised at approximately 25 daN with an ROP of approximately 1.5 m/h.

 Section 4 (16-30 min). When the sonde prototype inclination angle reached approximately 4°, the powered heaters configuration was changed. Four previously powered heater pairs were switched off, and four heater pairs on the opposite side were switched on.

 Based on the preliminary experimental results, the following conclusions can be drawn. To achieve the desired sonde prototype inclination, the WOB should be approximately 20 daN or higher. However, the test sonde weight was only 35 daN, which significantly reduced the range of the acceptable WOB values. To avoid a situation in which the entire sonde prototype weight would be at the bottom of the borehole, the WOB range was limited to 22-28 daN.

 When a 50% power limit was applied, the WOB stabilised at an ROP of approximately 1.5 m/h. Although WOB is not directly controlled, it depends on the ROP. However, constant WOB adjustments via ROP changes using a proportional-integral-derivative (PID) controller were not very effective because the transients significantly influenced the measured parameters. Therefore, in subsequent experiments, we decided to maintain a constant ROP despite potential WOB fluctuations.

 Because the coefficient *yoff* limits the maximum average PWM coefficient values, in practice, it limits the power consumption of the drill head, which, in turn, affects the maximum ROP. Preliminary experimental results showed that testing was meaningful only at WOB values close

 to the maximum. This means that at a certain *yoff* value, it is not possible to change the ROP over 360 a significant range. By analysing the "behaviour" of Eq. 3 we can conclude that at $y_{off} = 0.5$, the heat distribution is the most intense, and the assumed rate of change in borehole trajectory is also at its maximum. The limitation of the maximum borehole depth that can be obtained from the available ice blocks underscores its importance.

 Based on the above, we conducted a series of experiments with four different correction coefficient *T* values. The ROP was kept constant at 1.5 m/h. The WOB stabilised between 22 and 366 28 daN. The power consumption was limited to 50% by setting $y_{\text{off}} = 0.5$.

 According to the test plan, in the first approximately 300 mm of each experiment, the sonde prototype should drill with half of the heaters on one side turned off until the sonde inclination angle reaches approximately 4° (Ye et al., 2024). Subsequently, the automatic alignment mode will be enabled. The algorithm will recalculate the PWM coefficients of the heaters at 1-s intervals. It is worth noting that decreasing the PWM coefficient recalculation frequency (i.e., slowing the response to inclination angle changes) can influence the borehole deviation intensity. A decrease in the recalculation frequency is likely to result in a decrease in borehole deviation intensity.

5.3. Experimental results and analysis

 A total of four experiments were performed. The experimental recordings are shown in Fig. 16. As the values were recorded from the sensors at a frequency of once per second, the graphs are depicted with a 15-value moving-average filter. The graphs show trend lines for each experiment. For each trend line, the bold line indicates the accuracy limits according to the 379 inclinometer specifications $(\pm 0.2^{\circ})$.

(a) Borehole 1, $T = 0.5$, (b) Borehole 2, $T = 1$, (c) Borehole 3, $T = 1.5$ and (d) Borehole 4, $T = 2$

 Drilling of borehole 1 with *T* = 0.5 was unsuccessful owing to water leakage from the borehole; consequently, the results were difficult to analyse. The graph illustrates an approximation option intended to be obtained based on the analysis of the other three experiments. The experiment demonstrates that correction coefficient *T* affected how rapidly the borehole deviation changed over time. For clarity, the approximations of all four experiments are shown in Fig. 17.

To understand how crucial borehole deviations are for the passability of the sonde prototype,

it is necessary to analyse the results for the allowable deviation intensity according to the method

 described in Section 3. In the experiments, the automatic alignment length was approximately 0.5 m. For clarity, it was decided to divide this 0.5-m section of each borehole into several sections, for each of which the radius of curvature was determined. The option of partitioning the path not according to depth but rather according to inclination angle proved to be the most illustrative. Four sections were selected with the following inclination angle ranges: [4°-2.5°], [2.5°-1.5°], [1.5°-1°], and [1°-0.5°].

 The radius of curvature was determined for all four boreholes in each of the selected sections. To determine the radius, an additional angle (approximately in the middle of the range) was selected. The following additional angle values were selected for further calculations: 3.25° for the range [4°-2.5°], 2° for [2.5°-1.5°], 1.25° for [1.5°-1°], and 0.75° for [1°-0.5°]. Fig. 18 shows 402 the sonde trajectory for the $[4^{\circ}$ -2.5°] range in borehole 2 (*T* = 1).

404 **Fig. 18.** Borehole 2 ($T = 1$) trajectory within inclination angle range of $[4^{\circ} - 2.5^{\circ}]$

The sectional radius of curvature was calculated as follows:

abc ^R

$$
=\frac{abc}{4S}\tag{12}
$$

where *a*, *b* and *c* are the side lengths of triangle *ABC* and *S* is the area of triangle *ABC*.

407 The area of the triangle can be determined using Heron's equation:

$$
S = \sqrt{p(p-a)(p-b)(p-c)}\tag{13}
$$

408 where *p* is the semi-perimeter of a triangle.

409 The side lengths of triangle *ABC* can be determined using the Pythagorean theorem given

410 the coordinates of the points *A* (x_1 , z_1), *B* (x_2 , z_2) and *C* (x_3 , z_3) are known:

$$
a = \sqrt{(x_2 - x_1)^2 + (z_2 - z_1)^2}
$$
 (14)

$$
b = \sqrt{(x_3 - x_2)^2 + (z_3 - z_2)^2}
$$
 (15)

$$
c = \sqrt{(x_3 - x_1)^2 + (z_3 - z_1)^2}
$$
 (16)

 Knowing the coordinates of points *A*, *B*, and *C* for all sections using Eqs. 12-16, the radius of curvature of each section can be determined. Substituting the radius of curvature into Eq. 6, the maximum allowable sonde length satisfying the passability criteria for each segment can be determined. The resulting radius of curvature and maximum allowable sonde length values are presented in Table 8 and Fig. 19.

416 **Table 8**

417 Radius of curvature and maximum allowable sonde length

418

419 **Fig. 19.** Dependence of the maximum allowable sonde length at different borehole sections with the same inclination change

is structurally divided into several parts capable of deviating from each other (hinged joints).

- Allowing just a half-degree deviation of one part of the sonde from the other could increase
- its passability.
- In future work, we plan to conduct experiments on a larger scale (e.g., with a borehole depth
- of approximately 10 m) to refine the results in a deviation intensity range closer to that obtained
- with a real RECAS.
- **Data availability**
- All raw data can be provided by the corresponding authors upon request.

Author contributions

 Conceptualization: TPG, SMA, FX; hardware and equipment design: SMA, GD; software development SMA; resources and supplies: FX, GD, DZ, ZN; planning the experiment: SMA, TPG; assistance in preparing for experiments: FX, ZN, GD, DZ; conducting experiments and performed the measurements: SMA, FX; analysing the data: SMA, TPG; project administration: FX, ZN; financial management: YY, WT; supervision TPG; writing the manuscript draft: SMA, TPG; reviewing and editing the manuscript TPG; reviewing the manuscript: FX, GD.

Competing interests

The authors declare that they have no conflict of interest.

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